

UNSUPERVISED CLASSIFICATION OF SKELETAL FIBERS USING DIFFUSION MAPS

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ABSTRACT

In this paper, we propose an application of diffusion maps to fiber tract clustering in the human skeletal muscle. To this end, we define a metric between fiber tracts that encompasses both diffusion and localization information. This metric is incorporated in the diffusion maps framework and clustering is done in the embedding space using k-means. Experimental validation of the method is performed over a dataset of diffusion tensor images of the calf muscle of thirty subjects and comparison is done with respect to ground-truth segmentation provided by an expert.

Index Terms— DTI, Fibers, Diffusion Maps, Fiber Metrics, Human Skeletal Muscle

1. INTRODUCTION

Myopathies are neuromuscular diseases that result in a disorder in the musculoskeletal system of the human body whose symptoms are an atrophy and weakness of the muscles. They concern a significant part of the population: for instance, they affect 4 to 6 % of the European population (25 to 30 million persons). It is therefore important to harness the potential of emerging modalities like diffusion tensor imaging (DTI) to extract information about the impact of these diseases on the fiber architecture within the human skeletal muscle and to provide an assessment of the condition of a patient. A preliminary step towards this analysis is to classify the fibers obtained from DTI in anatomically coherent fiber bundles.

While DTI studies of the skeletal muscle [1, 2] focused on the evaluation of scalar values derived from DTI images like trace, fractional anisotropy and pennation angles, fiber segmentation has attracted less attention than in the study of human brain white matter, where a rich literature of unsupervised classification methods was proposed. For instance, the method presented in [3] introduced manifold learning techniques in the area of fiber bundling by relying on Laplacian Eigenmaps. In [4], spectral clustering along with the Hausdorff distance between fibers is considered. In [5], another

manifold learning technique is proposed based on a graph-based distance that captures local and global dissimilarities between curves and uses Locally Linear Embedding for clustering of the tracts. In [6], the Expectation-Maximization algorithm is used by considering Gamma distributions on the distance maps between fibers and cluster centers. The method proposed in [7] considers medoid-shift clustering combined with an Isomap-like manifold learning and suggested to include prior knowledge in the segmentation process using a white matter fiber atlas. Mean-shift was also used in [8] where each fiber is first embedded in a high dimensional space using its sequence of points, and adaptive mean-shift clustering was applied. A differential-geometric approach was recently proposed in [9] where clustering was done recursively using a consistency measure between fibers.

In this paper, we propose the combination of diffusion maps with a metric defined in the fiber domain to cluster the fibers of the human skeletal muscle. Diffusion maps were used for Orientation Distribution Function (ODF) segmentation in Q-ball images in [10], where spatial coherence was imposed using the Markovian relaxation of the affinity matrix. However the fiber domain provides no straightforward spatial neighborhood relationships like those given by the nearest neighbors in the 3D image grid. In the definition of the metric, we show how to impose spatial coherence in the fiber domain, while taking into account the information provided by the tensor field. The metric is used in the diffusion maps framework along with the k-means algorithm in the embedding space for clustering purposes. We build upon the method we proposed in [11], where we suggested an approach based on kernel principal component analysis for fiber clustering. In this work, diffusion maps are used to better reflect the manifold structure of the fiber tracts.

2. DIFFUSION MAPS

Diffusion maps [12] are a spectral embedding of a set X of n nodes, for which *local geometries* are defined by a kernel $k : X \times X \rightarrow \mathbf{R}$. The kernel k satisfies $k(x, y) \geq 0$, and

$k(x, y) = k(y, x)$. This kernel can be interpreted as an *affinity* between nodes. The resulting graph (an edge between x and y carries the weights $k(x, y)$) can be transformed into a reversible Markov chain by the so-called normalized graph Laplacian construction. A related construction was used in [13] to define a geometry on a set of observations, or trajectories. We define

$$s(x) = \sum_y k(x, y) \quad \text{and} \quad p(x, y) = \frac{k(x, y)}{s(x)}. \quad (1)$$

This new kernel is no longer symmetric, but it satisfies

$$\forall x, \sum_y p(x, y) = 1. \quad (2)$$

Therefore it can be interpreted as the probability of the transition from node x to node y in one time step, or a *transition kernel* of a Markov chain. It gives a diffusion operator

$$Pf(x) = \sum_y a(x, y)f(y)d\mu(y), \quad (3)$$

P is the Markov matrix with the entries $p(x, y)$ and its powers P^τ allow to propagate information through the Markov chain in τ timesteps according to the transition kernels. The operator P defines a geometry which can be mapped to an Euclidean geometry by an eigenvalue decomposition of P . The latter results in a sequence of eigenvalues $\lambda_1, \lambda_2, \dots$ and corresponding eigenfunctions Ψ_1, Ψ_2, \dots that fulfill $P\Psi_i = \lambda_i\Psi_i$. The diffusion map after τ timesteps $\Psi_\tau : X \rightarrow \mathbf{R}^w$ embeds each node $i = 1, \dots, n$ in the Markov chain into a w dimensional Euclidean space where the clustering of the data points can be done using k-means

$$i \mapsto \Psi_\tau(i) \triangleq \begin{pmatrix} \lambda_1^\tau \Psi_1(i) \\ \lambda_2^\tau \Psi_2(i) \\ \vdots \\ \lambda_w^\tau \Psi_w(i) \end{pmatrix} \quad (4)$$

A common choice for the kernel $k(\cdot, \cdot)$ is the Gaussian kernel, i.e. $k(x, y) = \exp\left(-\frac{d^2(x, y)}{2\sigma^2}\right)$, where d is a distance over the set X and σ a scale factor. Therefore, in order to apply the diffusion maps to fiber tracts, we define in the following a metric over the fiber domain.

3. A METRIC BETWEEN FIBER TRACTS

Instead of considering a fiber tract as a set of points, we will view it as a set of Gaussian probability distributions. Indeed, this viewpoint is justified by the fact that tractography is based on the integration of the field of principal directions of diffusion when the tensor field is assumed to be continuous (by means of interpolation). Therefore the tensor information can be kept along with the spatial positions obtained by tractography. So one can consider that each fiber tract F is represented

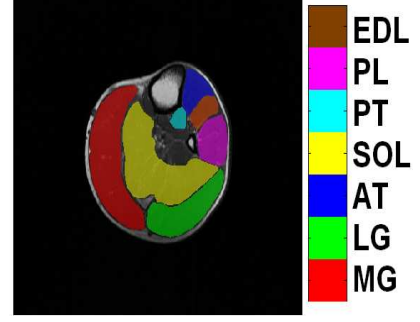


Fig. 1. An axial slice of a high-resolution T1-weighted image showing a manual segmentation of the calf muscle in seven groups

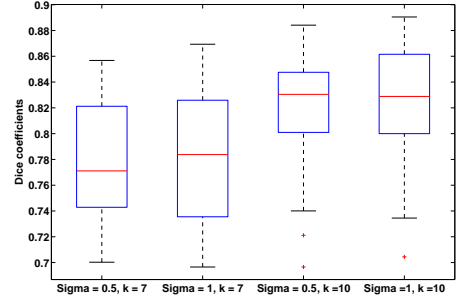


Fig. 2. Boxplots of dice overlap coefficients for the thirty subjects with different values of σ and k (the number of clusters). The box has lines at the lower quartile, median, and upper quartile values. The whiskers are lines extending from each end of the box to show the extent of the rest of the data. Outliers are data with values beyond the ends of the whiskers.

by a sequence of multivariate normal distributions $(p_i)_{i=1 \dots N}$ where N is the number of points of the fiber. The parameters $(\mathbf{x}_i, \mathbf{D}_i)$ of (p_i) are the spatial localization \mathbf{x}_i and the tensor \mathbf{D}_i at \mathbf{x}_i . More explicitly, given a diffusion (mixing) time t , the probability density function $p_i(\mathbf{y})$ at a position \mathbf{y} is given by the following expression:

$$p_i(\mathbf{y}) = \frac{1}{\sqrt{\det(\mathbf{D}_i)(4\pi t)^3}} \exp\left(-\frac{(\mathbf{y} - \mathbf{x}_i)^t \mathbf{D}_i^{-1} (\mathbf{y} - \mathbf{x}_i)}{4t}\right) \quad (5)$$

The main tool to define the fiber metric is the following affinity measure $C(p_i, p_j)$ defined as the normalized inner product between probability densities p_i and p_j :

$$C(p_i, p_j) = \frac{\int p_i(\mathbf{y})p_j(\mathbf{y})d\mathbf{y}}{\sqrt{\int (p_i(\mathbf{y}))^2 d\mathbf{y}} \sqrt{\int (p_j(\mathbf{y}))^2 d\mathbf{y}}} \quad (6)$$

Let us now consider two fiber tracts \mathbf{F}_1 and \mathbf{F}_2 represented by a set of probability densities $(p_i)_{i=1\dots N_1}$ (resp. $(\tilde{p}_i)_{i=1\dots N_2}$, where N_1 (resp. N_2) is the number of points of \mathbf{F}_1 (resp. \mathbf{F}_2). The affinity between probability densities in (6) admits a straightforward generalization to the fiber domain to obtain a similarity measure $\hat{C}(\mathbf{F}_1, \mathbf{F}_2)$ as follows:

$$\hat{C}(\mathbf{F}_1, \mathbf{F}_2) = \frac{1}{N_1} \frac{1}{N_2} \sum_{i=1}^{N_1} \sum_{j=1}^{N_2} C(p_i, \tilde{p}_j) \quad (7)$$

One can therefore derive the following metric d between fibers:

$$d(\mathbf{F}_1, \mathbf{F}_2) = \sqrt{2 - 2 \frac{\hat{C}(\mathbf{F}_1, \mathbf{F}_2)}{\sqrt{\hat{C}(\mathbf{F}_1, \mathbf{F}_1)} \sqrt{\hat{C}(\mathbf{F}_2, \mathbf{F}_2)}}} \quad (8)$$

It turns out that $d(\mathbf{F}_1, \mathbf{F}_2)$ has an explicit expression. Indeed, one can show (computations are omitted) that we can derive a closed form expression of $C(p_i, \tilde{p}_j)$ for multivariate normal distributions:

$$C(p_i, \tilde{p}_j) = 2\sqrt{2} \frac{\det(\mathbf{D}_i)^{\frac{1}{4}} \det(\mathbf{D}_j)^{\frac{1}{4}}}{\sqrt{\det(\mathbf{D}_i + \mathbf{D}_j)}} \times \exp\left(-\frac{1}{4t} (\mathbf{x}_i - \mathbf{x}_j)^t (\mathbf{D}_i + \mathbf{D}_j)^{-1} (\mathbf{x}_i - \mathbf{x}_j)\right) \quad (9)$$

The computation of the metric $d(\mathbf{F}_1, \mathbf{F}_2)$ between fibers is straightforward using (7) and (8). Note how this formulation provides a natural way to take spatial relationships into account while keeping the information provided by the tensor field.

4. EXPERIMENTS AND RESULTS

Thirty subjects (twenty healthy subjects and ten patients affected by myopathies) underwent a diffusion tensor imaging of the calf muscle using a 1.5 T MRI scanner. The following acquisition parameters were used : repetition time (TR)= 3600 *ms*, echo time (TE) = 70 *ms*, slice thickness = 7 *mm* and a b value of 700 *s.mm*⁻² with 12 gradient directions and 13 repetitions. The size of the obtained volumes is 64 × 64 × 20 voxels with a voxel resolution of 3.125 *mm* × 3.125 *mm* × 7 *mm*. We acquired simultaneously high-resolution T1-weighted images that were segmented manually by an expert into seven muscle groups to provide the ground truth. To give an idea about the muscle architecture in the calf, we present in [Fig.1] a manual segmentation overlaid on an axial slice of a high-resolution T1-weighted image. The following muscle groups are considered: the soleus (SOL), lateral gastrocnemius (LG), medial gastrocnemius (MG), posterior tibialis (PT), anterior tibialis (AT), extensor digitorum longus (EDL), and the peroneus longus (PL). We manually delineated a region of interest (ROI) for

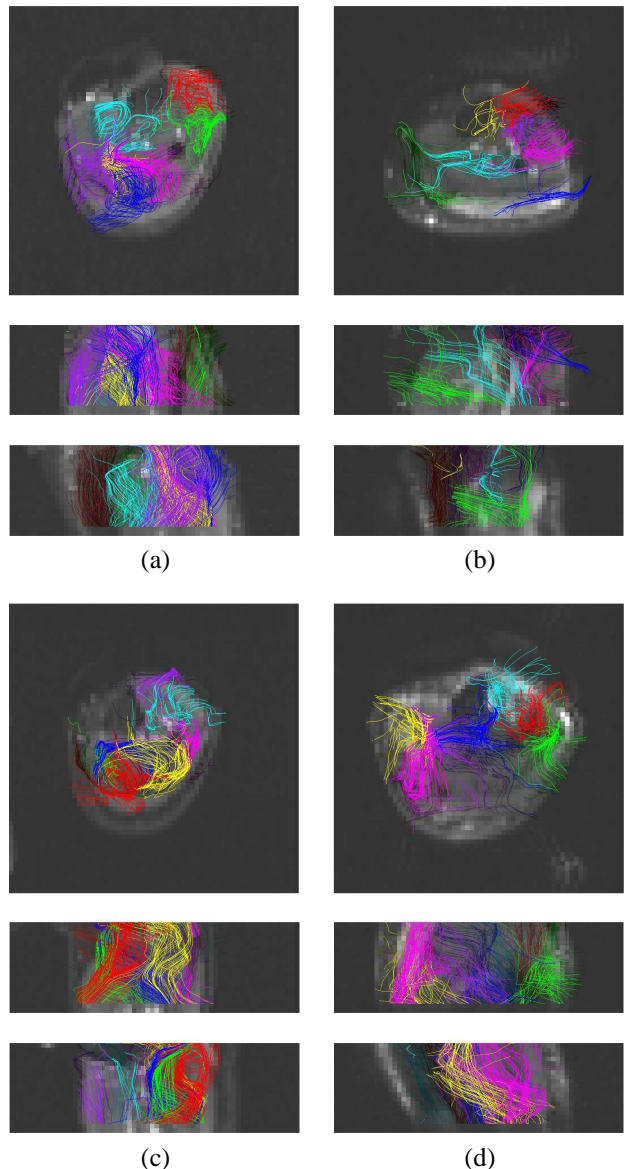


Fig. 3. Axial, coronal and sagittal views of tractography segmentation in 7 classes overlaid on diffusion-free (B0) images for (a), (c) two healthy subjects (b), (d) two diseased subjects

fiber tracking [14] and the fibers with a majority of points lying outside of the ROI were discarded. The obtained manual segmentations of the T1-weighted images were downsampled to the resolution of the diffusion images and used to provide a ground-truth segmentation of the fiber tracts as follows: for each fiber, the number of voxels crossed by the fiber and belonging to each muscle group were counted. Then the fiber was assigned to the class with the majority vote.

In order to quantitatively evaluate the proposed method, we measure the dice overlap coefficient of the obtained seg-

mentation with the ground-truth segmentation provided by the clinician. We tested the clustering method at two levels: for 7 and 10 clusters. The dimension of the diffusion maps embedding w was set to the number of clusters. The number of timesteps τ in (4) was set to $\tau = 1$. We tested two values for the scale parameter of the Gaussian kernel: $\sigma = \{0.5, 1\}$ and in all the experiments, the diffusion time t was set to $t = 2 \cdot 10^4$. The clustering in the embedding space is done using k-means with 50 restarts and taking the clustering result with the least distortion. Distortion is computed as the ratio of intra-class and inter-class variances.

In [Fig.2], we present the boxplots of the dice overlap coefficients for the thirty subjects, using the different values of σ for 7 and 10 clusters. We can note that the quantitative results are rather satisfactory. For example, with the parameter σ set to $\sigma = 1$, we obtain a mean dice overlap coefficient of 0.78 (resp. 0.82) and a standard deviation of 0.05 (resp. 0.045) for 7 (resp. 10) classes. For a qualitative assessment, we show in [Fig.3] the obtained fiber classification in 7 clusters for two healthy and two diseased subjects. It is important to note in this setting that the diffusion images of the skeletal muscle are intrinsically noisier than brain images due to the short spin-spin (T2) relaxation time of the muscle tissue. Therefore the obtained fiber tracts are rather noisy, especially for diseased patients where the fat artifact is stronger. Despite the low quality of the tractography, our algorithm could still segment it in coherent fiber bundles.

5. CONCLUSION

We proposed a diffusion maps based method for fiber clustering in the human skeletal muscle. The main ingredient of the algorithm is the definition of a metric between fibers that encompasses spatial and diffusion information. The experimental validation shows promising results both for healthy and diseased subjects. It would be interesting to perform statistical analysis of diffusion properties within each fiber bundle and assess the changes induced by myopathies.

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