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On the Near-Field Sampling and Truncation Errors in Planar Time-Domain Near-Field to Far-Field Transformation

Mohammed Serhir*

Abstract—This paper studies the effect of three important parameters in planar time-domain (TD) near-field (NF) to far-field (FF) transformation. These parameters are the NF spatial sampling, the NF measurement distance and the scan surface truncation. The effect of these parameters over the TD FF accuracy are difficult to predict for Ultra Wide Band antennas. In this paper we aim to choose the optimum NF measurement parameters guaranteeing accurate calculation of the time-domain far-field. This allows the optimization of the computation time and memory requirements. Computations using analytic array of elementary dipoles radiation pattern are used to study the impact of each parameter in time-domain near-field antenna measurement. The comparison of the far-field results are presented in time and frequency domains. In particular, it is shown that the choice of the measurement distance and the size of the scan surface decide predominantly on the frequency band of accurate FF calculation. The used formalism in this paper for the NF to FF transformation is based on the Green's function.

1. INTRODUCTION

The Ultra Wide Band (UWB) antennas operating over large frequency bandwidth have attracted a lot of interest over wide telecommunication applications [1-5]. The measurement of the radiation pattern of these antennas has to be carried in a wide frequency band, which is time consuming. For these antennas, the time-domain (TD) techniques seem to be more adapted than frequency-domain (FD) techniques. Indeed, using a short pulse, one can measure the antenna transient response covering the frequency band of interest. This measurement is fulfilled using near-field (NF) or far-field (FF) techniques [6].

In TD FF measurements we record the antenna under test (AUT) transient response when it is excited by a specific pulse. The excitation pulse has to cover the frequency band of interest and supply the AUT with enough power that allows the measurement with acceptable signal to noise ratio at far-field distances. In TD NF techniques the tangential components of radiated field are collected in the antenna vicinity over a scan surface (planar, cylindrical or spherical). Then, the measured data are transformed to calculate the asymptotic behavior of the antenna far-field. For NF measurement, we use pulse generators providing a trade-off between the output voltage magnitude and a short pulse rise-time for wide frequency band characterization.

For accuracy improvement, the post processing tools such as TD gating technique are used to filter out the multiple reflections occurring during the measurement [7]. The TD techniques allow the radiation pattern measurement in non-anechoic environment as presented in [8]. These are well adapted for the parasitic electromagnetic radiation emitted from electronic devices for electromagnetic compatibility purpose [9]. Also, using TD techniques one can measure the radiation pattern of radar structures fed by non-sinusoidal excitation signals. Particularly, when the feeding system is integrated in the radiating antennas for radar applications.

The main difficulty related to the practical use of NF TD techniques concerns the ability to manage the quantity of measured data. The required computation time and memory storage became problematic

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* Corresponding author: Mohammed Serhir (mohammed.serhir@supelec.fr).

Laboratoire Genie électrique et électronique de Paris (GeePs) (UMR 8507 CentraleSupélec - CNRS UPSud - UPMC) 11 rue Joliot-Curie - Plateau de Moulon 91192 Gif sur Yvette Cedex - France.

for large measurement surface and long-time window (long transient response). The quantity of NF data depends on the used time and spatial sampling criteria. These are determined based on the AUT excitation signal maximum frequency as presented in [10]. Authors in [11-13] present a different NF sampling strategy that aims at representing the NF measurement data using plane polar samples allowing a minimum redundancy in NF sampling. In the FD, Wang in [14] presents a detailed analysis on the theory and practices for planar near-field measurement. The sampling strategies, the NF probe characteristics, the filtering of the NF data and the evanescent modes effect have been addressed. Authors of [15-18] have presented some experimental setups for NF or FF antenna measurement. These papers did not present the sampling strategies used in the NF or FF measurements.

In planar TD near-field antenna measurement, the sampling approach is based on the assumption that the time signal is band-limited to a maximum angular frequency $\omega_{max} = 2\pi c/\lambda_{min}$. This leads to the NF sampling criterion $\Delta y = \Delta z = \lambda_{min}/2$ and the AUT excitation pulse defines approximately the frequency band of interest (minimum and maximum frequencies). This assumption gives a reduced view of the reality of TD NF measurement practices. Considering the spatial sampling criterion based on the highest frequency of the AUT excitation signal ($\lambda_{min}/2$), as presented in [10], does not guarantee the accuracy of the TD far-field calculation. Indeed, the AUT *directivity* depends on the frequency and using the same measurement surface for time-domain FF calculation leads to a frequency dependent truncation error. Also, the NF measurement has to be carried in the radiating NF zone (Fresnel zone). This Fresnel zone distance depends on the AUT dimensions and the operating frequency. For NF TD technique, the measurement distance has to be adapted to avoid the reactive NF zone for low frequencies. These three parameters are responsible of the TD FF errors.

In this paper we propose to determine the AUT TD FF using different sampling criteria and for several NF measurement distances. By comparing the far-field results, we show that the TD FF errors are resulting from NF evanescent modes with low measurement distances, under-sampling and scan surface truncation errors. It is difficult to distinguish between these errors in the TD FF directly. The frequency-domain (FD) comparisons are presented to make out the effect of each error.

In the NF to FF transformation scheme we use the reconstruction formula to rigorously interpolate the NF in the time-domain. We propose a simple and rigorous formulation to calculate the E-field time derivative from the measured E-field as complementary development of the analysis presented in [10]. The computation scheme for NF to FF field transformation is validated using analytic radiating array composed of infinitesimal dipoles. The paper is structured as follows. In Section II, the NF to FF formalism based on the Green's function is described and the different formulation needed for our analysis are commented. In Section III, we present the transformation results and a comparison of the calculated far-field with the actual one in the time and the frequency domains. In Section IV, recommendations and concluding remarks are presented.

2. TIME-DOMAIN NEAR-FIELD TO FAR-FIELD TRANSFORMATION

In this section, we first recall the equations expressing the NF to FF transformation based on the Green's formulation. The detailed developments can be found in [10]. Then, we present how to calculate rigorously the E-field time derivative using the reconstruction formula. Finally, we present the analytic expressions of infinitesimal dipole radiated field in the TD when it is excited by modulated Gaussian pulse. This infinitesimal dipole is used to generate the TD radiation pattern of our AUT composed of 40 infinitesimal dipoles.

2.1. Time-domain near-field to far-field formalism

In this paper we use the time-domain near-field to far-field transformation algorithm based on the Green's function representation [10]. The antenna NF tangential components E_y and E_z are collected over the plane $x = x_{meas}$. Equation (1) expresses the antenna far-field $\vec{F}(\theta, \phi, t)$ in the direction (θ, ϕ) (spherical coordinates associated with the Cartesian coordinates) as a function of the time derivative of the tangential components of the measured NF E_{meas} .

$$\vec{F}(\theta, \phi, t) = -\frac{1}{2\pi c} \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} \vec{e}_r \times \left[\vec{e}_x \times \frac{\partial \vec{E}_{meas}}{\partial t}(\vec{r}_0, t + \vec{e}_r \cdot \vec{r}_0/c) \right] dy_0 dz_0$$

with $\vec{F}(\theta, \phi, t) = \lim_{r \rightarrow \infty} r \vec{E}(\vec{r}, t + r/c)$

(1)

The measurement surface is defined by $-D_{max} \leq y, z \leq D_{max}$, and (1) is expressed in a truncated form as

$$\vec{F}(\theta, \phi, t) = -\frac{1}{2\pi c} \int_{-D_{max}}^{+D_{max}} \int_{-D_{max}}^{+D_{max}} \vec{e}_r \times \left[\vec{e}_x \times \frac{\partial \vec{E}_{meas}}{\partial t}(\vec{r}_0, t + \vec{e}_r \cdot \vec{r}_0/c) \right] dy_0 dz_0$$
(2)

The tangential components of the measured field vector \vec{E}_{meas} are collected at a regular grid described by $\vec{r}_0 = x_{meas} \vec{e}_x + y \vec{e}_y + z \vec{e}_z$ with $-D_{max} \leq y, z \leq +D_{max}$. Using the sampling theorem [10], we transform (2) to the following double summation

$$\vec{F}(\theta, \phi, t) = -\frac{1}{2\pi c} \sum_{n=-N_y}^{N_y} \sum_{m=-N_z}^{N_z} \vec{e}_r \times \left[\vec{e}_x \times \frac{\partial \vec{E}_{meas}}{\partial t}(\vec{r}_{0mn}, t + \vec{e}_r \cdot \vec{r}_{0mn}/c) \right] \Delta y_0 \Delta z_0$$

where $\vec{r}_{0mn} = x_{meas} \vec{e}_x + m \Delta y \vec{e}_y + n \Delta z \vec{e}_z$, $\vec{e}_r = \cos(\phi) \sin(\theta) \vec{e}_x + \sin(\phi) \sin(\theta) \vec{e}_y + \cos(\theta) \vec{e}_z$

(3)

We have developed a Matlab routine expressing (3) to calculate the FF using NF data calculated at several measurement distances $x = x_{meas}$ with different sampling criterion $\Delta y, \Delta z$. In (3), the first step in NF to FF transformation is the calculation of the time derivative of the measured NF at the instant $\frac{t + \vec{e}_r \cdot \vec{r}_{0mn}}{c}$. The accuracy of the result depends on the chosen interpolation method. In our analysis, we will use the reconstruction formula to determine the time derivative of the measured field and to interpolate the field at the required instants.

2.2. The reconstruction formula

Let us define a function $f(t)$ where f_ω is its Fourier transform. $f(t)$ is a band limited function if for $\omega \geq \omega_{max}$

$$f_\omega = -\frac{1}{2\pi} \int_{-\infty}^{+\infty} f(t) \exp(j\omega t) dt = 0$$
(4)

The reconstruction formula allows the exact interpolation of the band limited function $f(t)$ using the discrete points $f(t_0 + l\Delta t)$. $f(t)$ is expressed for every $t \in [t_0, t_0 + (N_t - 1)\Delta t]$ using the cardinal series as

$$f(t) = \sum_{l=0}^{N_t-1} \text{sinc} \left(\pi \left(\frac{t - (t_0 + l\Delta t)}{\Delta t} \right) \right) f(t_0 + l\Delta t)$$
(5)

Using the discrete measurement samples $\vec{E}_{meas}(t_0 + l\Delta t)_{1 \leq l \leq N_t-1}$, one can express accurately $\vec{E}_{meas}(t)$ for every $t \in [t_0, t_0 + (N_t - 1)\Delta t]$. To do this, the Nyquist sampling criterion $\Delta t = \pi/\omega_{max}$ has to be respected. The reconstruction formula is used to interpolate the measured E-field as:

$$\vec{E}_{meas}(\vec{r}_{0mn}, t) = \sum_{l=0}^{N_t-1} h(t) \vec{E}_{meas}(\vec{r}_{0mn}, t_0 + l\Delta t)$$

with $h(t) = \frac{\sin \left(\pi \frac{t - (t_0 + l\Delta t)}{\Delta t} \right)}{\pi \frac{t - (t_0 + l\Delta t)}{\Delta t}}$

(6)

For $t_0 \leq t \leq t_0 + (N_t - 1)\Delta t$, the time derivative of the E-field is expressed rigorously as

$$\frac{\partial \vec{E}_{meas}(\vec{r}_{0mn}, t)}{\partial t} = \sum_{l=0}^{N_t-1} \frac{\partial h(t)}{\partial t} \vec{E}_{meas}(\vec{r}_{0mn}, t_0 + l\Delta t)$$

where

$$\frac{\partial h(t)}{\partial t} = \frac{1}{t - (t_0 + l\Delta t)} \left(\cos\left(\pi \frac{t - t_0}{\Delta t} - l\right) - h(t) \right) \quad (7)$$

If the sampling Nyquist criterion is respected, (6) and (7) interpolate the E-field and its time derivative. Here, we consider the antenna under test (AUT) composed of infinitesimal dipoles distributed over the plane $x = 0$ as shown in Fig. 1. Each dipole is excited by a pulse and the TD NF is collected over the plane $x = x_{meas}$ at regularly spaced positions. In the next paragraph, we express the analytical expression of the field radiated by an elemental dipole.

2.3. Transient radiation of an infinitesimal dipole

Let us consider a z-polarized elemental dipole placed at the origin of the coordinate system. This dipole is excited by $e(t)$, a sinusoidal current modulated by a Gaussian pulse written as

$$e(t) = e_0 \sin(\beta t) \exp(-\alpha t^2)$$

whith $\alpha = 2/\tau^2$

(8)

The transient radiated fields E_r and E_θ are written in the spherical coordinates system

$$E_r(r, \theta, \phi, t) = \frac{2\eta}{4\pi r^2} \cos(\theta) \left[\frac{\partial e(t - r/c)}{\partial t} + \frac{c}{r} e(t - r/c) \right]$$

$$E_\theta(r, \theta, \phi, t) = \frac{\eta}{4\pi r} \sin(\theta) \left[\frac{\partial^2 e(t - r/c)}{c\partial t^2} + \frac{\partial e(t - r/c)}{r\partial t} + \frac{e(t - r/c)}{r^2} \right] \quad (9)$$

with

$$\frac{\partial e(t)}{\partial t} = e_0 [\beta \cos(\beta t) - 2\alpha t \sin(\beta t)] \exp(-\alpha t^2)$$

$$\frac{\partial^2 e(t)}{\partial t^2} = e_0 \left[(4\alpha^2 t^2 - \beta^2 - 2\alpha) \sin(\beta t) - 4\alpha\beta t \cos(\beta t) \right] \exp(-\alpha t^2) \quad (10)$$

We have used (8)-(10) to generate the tangential components E_z and E_y radiated by 40 elementary dipoles placed at the plane $x = 0$. The distance between dipoles is 5cm , $\beta = 4\pi 10^9 \text{rad/s}$ and $\tau = 0.8 \cdot 10^{-9} \text{s}$. The dipole distribution is described in Fig. 1. The measurement surface is limited by D_{max} as shown in Fig. 2 and the TD radiation pattern in the cut planes $y_{meas} = 0$ and $z_{meas} = 0$ are presented in Fig. 3.

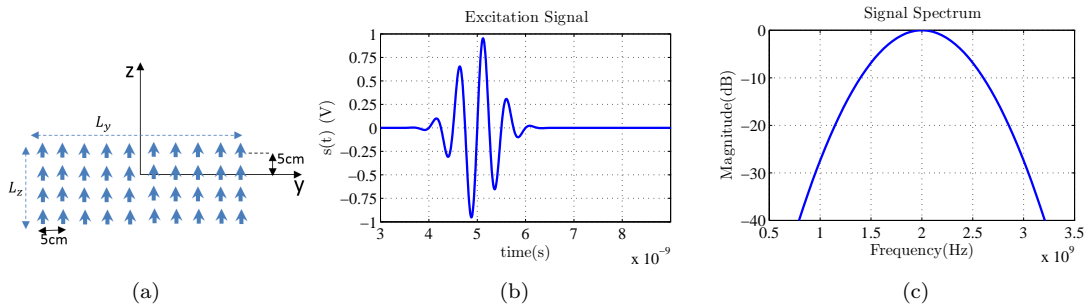


Figure 1: The time-domain excitation signal (b) applied to each of the 40 dipoles composing the AUT (a) and the magnitude of the excitation signal spectrum (c). The maximum of the spectrum is at 2GHz .

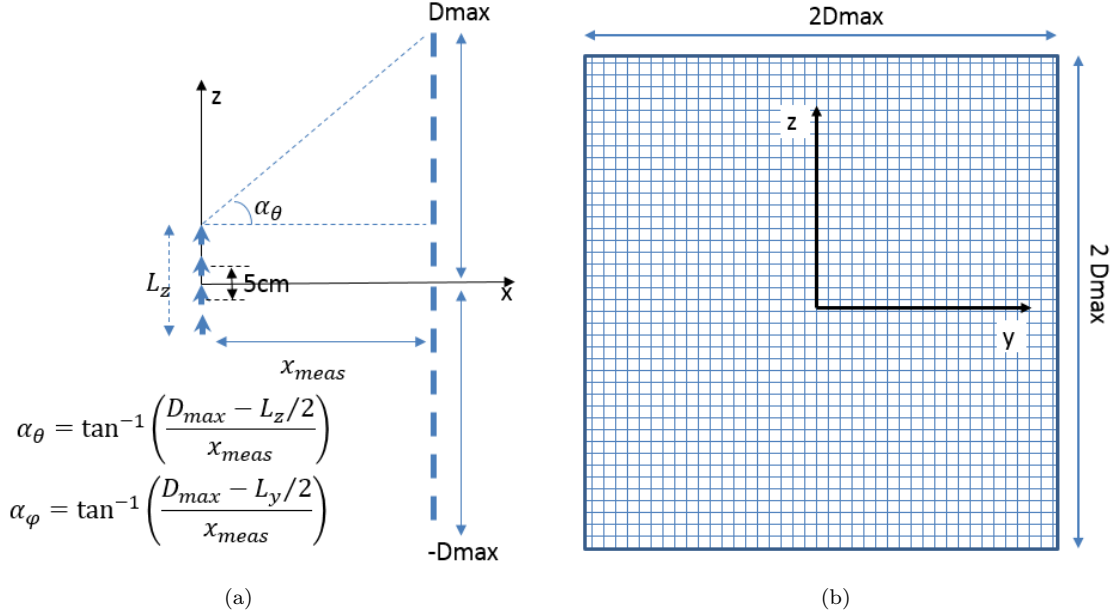


Figure 2: Near-field measurement grid at the distance x_{meas} from the AUT. The tangential components E_y and E_z are regularly recorded over a square surface in the zy plane.

3. NUMERICAL RESULTS

In this section we are interested in evaluating the accuracy of the time-domain (TD) FF as a function of the spatial sampling criterion Δy and Δz . The antenna under test (AUT) is composed of 40 elementary dipoles excited by a sinusoidal current modulated by a Gaussian pulse. The NF measured at the distance $x_{meas} = 50cm = 5\lambda_{3GHz}$ ($x_{meas} = 5\lambda_{1GHz}/3$) is presented in the TD in Fig. 3 and in the FD in Fig. 4.

3.1. The near-field measurement surface truncation and the sampling criterion

3.1.1. The time-domain far-field results comparison

In the planar rectangular frequency-domain measurement technique, the NF is spatially sampled using the Nyquist rule $\Delta y = \Delta z = \lambda/2$ with λ being the working wavelength. As presented in [10] the TD NF is spatially sampled based on the AUT excitation signal maximum frequency $\Delta y = \Delta z = \lambda_{min}/2 = c\pi/\omega_{max}$. For a short pulse (UWB antenna), the maximum frequency can be F_{-3dB} , F_{-10dB} , F_{-20dB} , F_{-30dB} . F_{-XdB} is the frequency for which the magnitude of the excitation pulse spectrum is lower by X value compared with the normalized maximum level ($0dB$) of the central frequency. For our case of study, as it is seen in Fig. 1, $F_{-3dB} \approx 2.3GHz$, $F_{-6dB} \approx 2.4GHz$, $F_{-10dB} \approx 2.6GHz$, $F_{-20dB} \approx 2.8GHz$ and $F_{-30dB} \approx 3GHz$. The maximum magnitude of the excitation signal spectrum corresponds to the central frequency $F_{0dB} = f_0 = 2GHz$. We propose to express $F_{-3dB} \approx 1.15f_0$, $F_{-6dB} \approx 1.2f_0$, $F_{-10dB} \approx 1.3f_0$, $F_{-20dB} \approx 1.4f_0$, $F_{-30dB} = 1.5f_0$. In order to study the effect of NF spatial sampling criterion over the calculated FF, we use χ to parameterize the spatial sampling $\Delta y_\chi = \Delta z_\chi = \lambda_0/2\chi$, where $\chi = 1.1, 1.2, 1.3, 1.4, 1.5$ and $\lambda_0 = c/f_0$. By comparing the far-field calculated using different χ , we identify the influence of the chosen maximum frequency on the accuracy of the calculated AUT FF. The NF time-axis is sampled using $\Delta t = \frac{1}{3F_{-30dB}}$ to prevent the time-domain aliasing error.

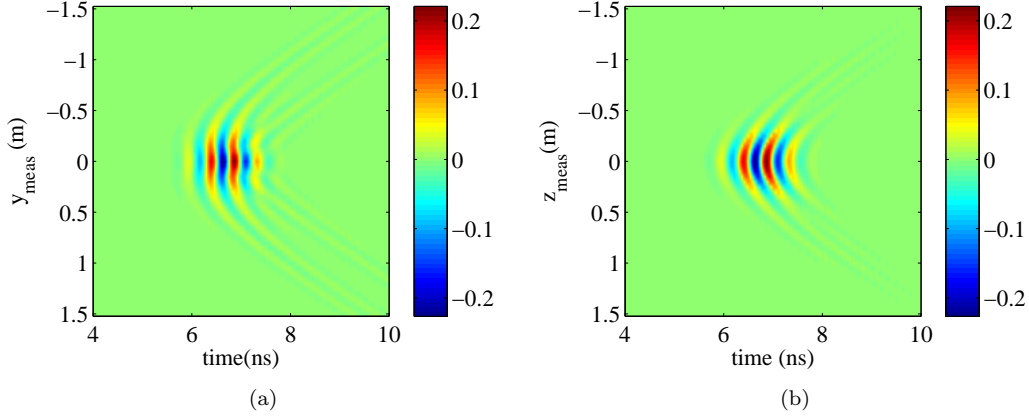


Figure 3: The E_z (V/m) near-field radiated by the AUT (40 dipoles) as a function of the time. (a) The E_z (V/m) at the plane cut $z_{meas} = 0$. (b) The E_z (V/m) at the plane cut $y_{meas} = 0$.

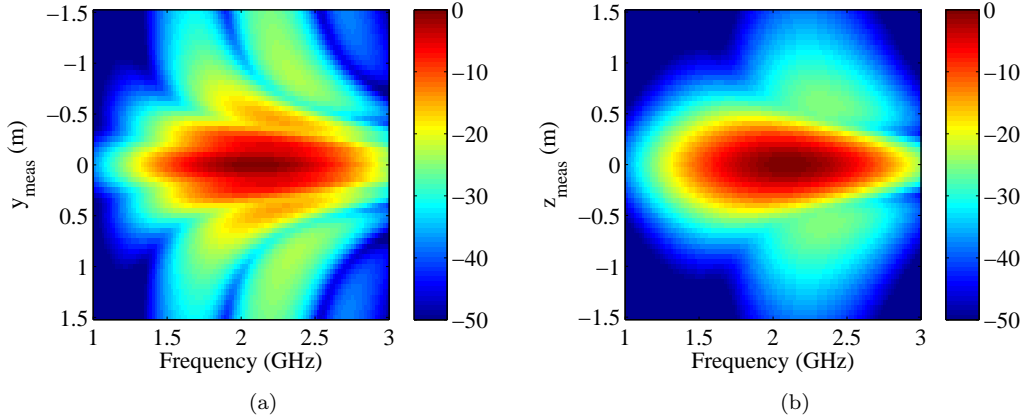


Figure 4: The normalized E_z (dB V/m) NF measured at ($x_{meas} = 50cm$) radiated by the AUT (40 dipoles) as a function of the frequency. (a) The E_z (dB(V/m)) at the plane cut $z_{meas} = 0$. (b) The E_z (dB(V/m)) at the plane cut $y_{meas} = 0$.

Over the planar surface at the distance $x_{meas} = 50cm$ from the AUT, we calculate the near-field at regularly spaced points with $\Delta y_\chi = \Delta z_\chi = \lambda_0/2\chi$ and $D_{max} = 150cm$ ($10\lambda_0$). Then, using (3) and (7), we calculate the FF at the directions $(\theta = \pi/2, \phi = 0)$, $(\theta = \pi/3, \phi = 0)$, and $(\theta = \pi/2, \phi = \pi/6)$ for $\chi = 1.1, 1.2, 1.3, 1.4, 1.5$. The E_z component of the FF is presented in Fig. 5 (a-c-e) and compared with the reference FF determined directly from (9) and (10) for r going to infinity. This actual far-field is labeled Ref in Fig. 5. The differences between the calculated FFs and the actual one are quantified using the error expressed in (11). $E_{NFtoFF}(\theta, \phi, t)$ is the field calculated using NF to FF transformation and $E_{Ref}(\theta, \phi, t)$ is the actual far-field.

$$Error(\theta, \phi, t) = 100 \times \frac{E_{NFtoFF}(\theta, \phi, t) - E_{Ref}(\theta, \phi, t)}{\max(E_{Ref}(\theta, \phi, t))_{t_0 \leq t \leq t_0 + (N_t - 1)\Delta t}} \quad (11)$$

The errors of the curves in Fig. 5(a) are presented in Fig. 5(b) for different χ . The errors of the comparisons presented in Fig. 5(c) are plotted in Fig. 5(d). Fig. 5(f) presents the errors of Fig. 5(e). From Figs. 5 (b-d-f) the early-time far-field introduced in [10] as being the part of the radiated FF without the truncation error is *visually* observed in Fig. 5(e). The measurement surface truncation effect is visible at $t = 7ns$ and $10ns \leq t \leq 13ns$.

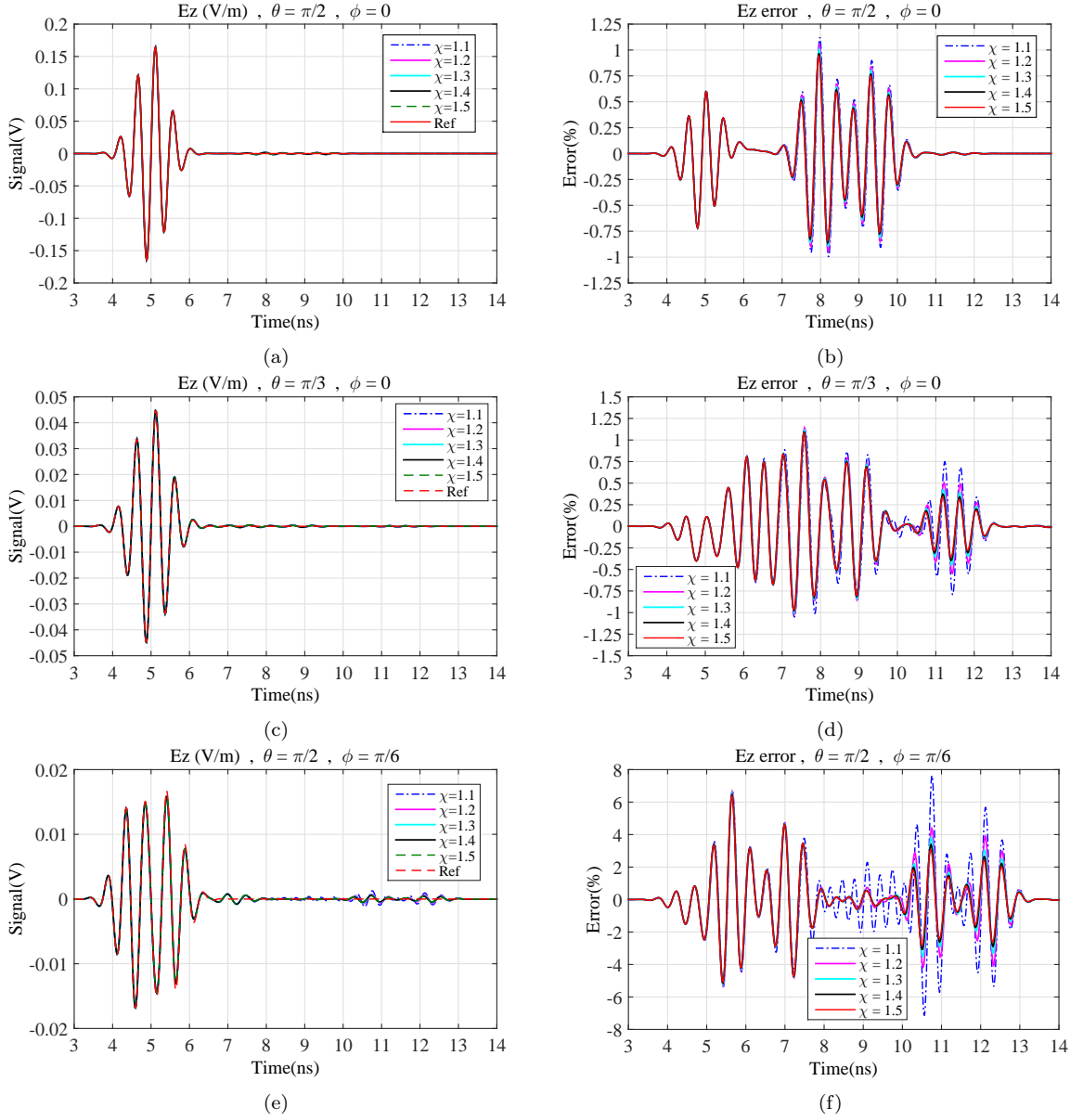


Figure 5: Comparison of the NF to FF transformation results for different sampling criteria $\Delta y = \Delta z = \lambda_0/2\chi$, $D_{max} = 150cm$ and $x_{meas} = 50cm$. The TD FF E_z component at (a) $\theta = \pi/2$ and $\phi = 0$, (c) $\theta = \pi/3$ and $\phi = 0$ (e) $\theta = \pi/2$ and $\phi = \pi/6$. The errors of Figs. (a-c-e) are respectively (b) $\theta = \pi/2$ and $\phi = 0$, (d) $\theta = \pi/3$ and $\phi = 0$ (f) $\theta = \pi/2$ and $\phi = \pi/6$.

As explained in [10], the effect of the truncation error arrives chronologically after the actual FF signal. This is presented in [10] for a point source. Nevertheless, in Fig. 5 (b-d-f), we notice quantitative differences between the calculated far-fields (FFs) and the actual one even in the time portion of the radiation pattern attributed to early-time far-field ($4ns \leq t \leq 6ns$).

In order to understand the origin of the errors for $4ns \leq t \leq 6ns$, we have used a larger measurement surface to calculate the FF ($D_{max} = 300cm$) with the same sampling conditions. The obtained results have shown the same error level for $4ns \leq t \leq 6ns$. These errors are not attributed to the size of the measurement surface. However, we have applied the same analysis (same excitation pulse, same sampling conditions, same measurement distance) for a smaller antenna (4×4) composed of 16 dipoles with $5cm$ between dipoles and $D_{max} = 150cm$, the error level is smaller for $4ns \leq t \leq 6ns$. Moreover, this decreasing tendency is confirmed for 4 dipoles (2×2). The errors for $4ns \leq t \leq 6ns$ is directly linked

to the size of the AUT.

As presented in Fig. 5(b-d-f), the error levels depend on the FF observation point (θ, ϕ) . The angular FF directions free from truncation error depends on three parameters, namely the measurement distance ($x_{meas} = 50cm$), the AUT size ($L_y = 45cm$ and $L_z = 15cm$) and the measurement surface dimensions ($D_{max} = 150cm$). Here, the **critical angle** is defined by $\alpha_\theta = 70deg$ and $\alpha_\phi = 68deg$ as expressed in Fig. 2. This allows an angular FF area free from truncation errors for $30deg \leq \theta \leq 150deg$ and $-68deg \leq \phi \leq 68deg$. This provides an indication and not the exact angular area, especially when the measured field level in the edge of the measurement surface is of comparable levels with the maximum measured field.

In Fig. 6 we show the FF errors calculated at the principal plane cuts $\theta = \pi/2$ with $-\pi/2 \leq \phi \leq \pi/2$ and $\phi = 0$ with $0 \leq \theta \leq \pi$. The presented errors are for $\chi = 1.2, 1.3$ and 1.5 . It is seen from Figs. 6 (c) and (f) that the NF sampled using $\chi = 1.2$ is under-sampled since the observable oscillations are due to the aliasing errors. In Figs. 6 (a-b-d-e) we have less oscillations. The errors behavior do not reveal early-time far-field region where the truncation error happens later in time compared with the actual FF. The errors level for $4ns \leq t \leq 6ns$ (actual far-field) is of comparable level with the errors for $7ns \leq t \leq 10ns$. The errors for $0 \leq \theta \leq 30deg$, $150deg \leq \theta \leq 180deg$, $-90deg \leq \phi \leq -68deg$, and $68deg \leq \phi \leq 90deg$ are due to the truncation of the measurement surface as predicted by $\alpha_\theta = 70deg$ and $\alpha_\phi = 68deg$. In addition, the errors for $\chi = 1.5$ and $\chi = 1.3$ have comparable behavior as it is seen from Figs. 6 (a-b-d-e). Consequently, comparing the TD FF results for this AUT, the weighting factor $\chi = 1.3$ ($F_{-10dB} \approx 1.3f_0$) allows a comparable accuracy as $\chi = 1.5$ ($F_{-30dB} \approx 1.5f_0$).

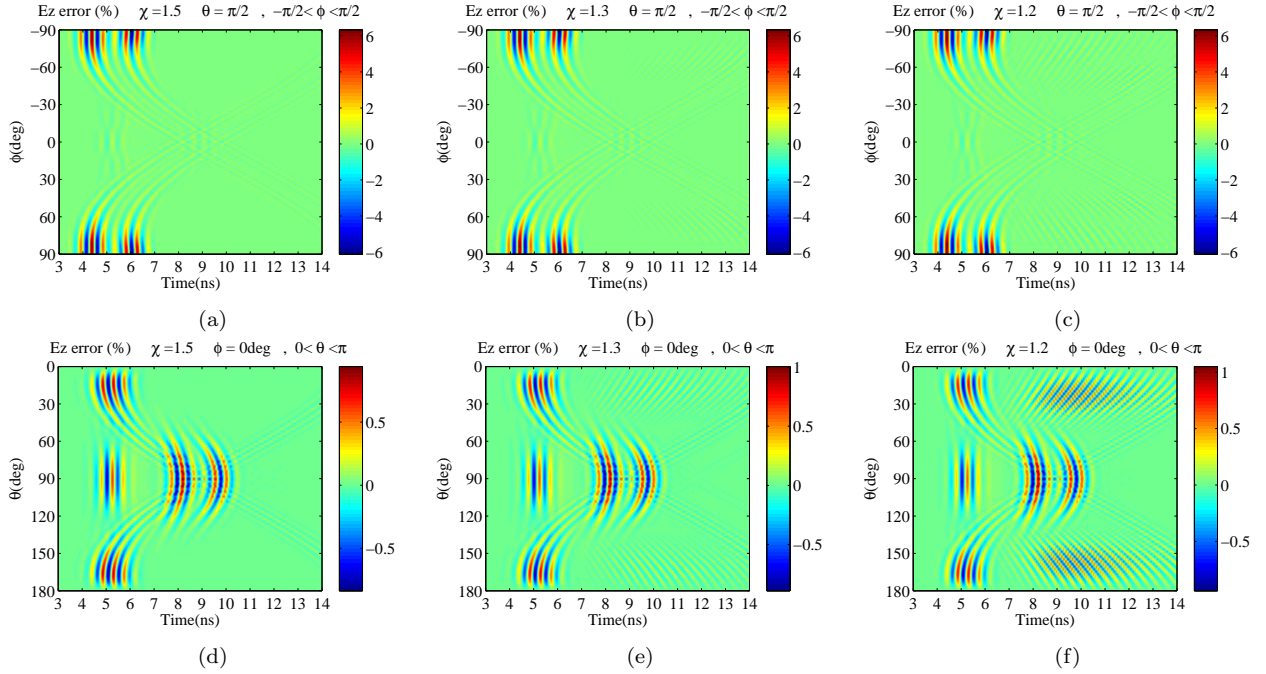


Figure 6: The FF Ez component error as a function of time for the plane cut $\theta = \pi/2$. (a) for $\chi = 1.5$, (b) for $\chi = 1.3$, (c) for $\chi = 1.2$. The Ez error as a function of time for the plane cut $\phi = 0$, (d) for $\chi = 1.5$, (e) for $\chi = 1.3$, (f) for $\chi = 1.2$.

3.1.2. The frequency-domain far-field results comparison

Using the NF sampling criterion $\Delta y_\chi = \Delta z_\chi = \lambda_0/2\chi$ $x_{meas} = 50cm$ and $D_{max} = 150cm$ we compare the calculated far-fields in the frequency-domain (FD). These FFs are set by Fourier transforming the previously calculated TD far-fields. The comparisons are carried out at the principal plane cuts $\theta = \pi/2$ and $\phi = 0$ at F_{-10dB} ($1.4GHz$ and $2.6GHz$), F_{-20dB} ($1.2GHz$ and $2.8GHz$), F_{-30dB} ($1GHz$ and $3GHz$) for different χ .

It is seen in Fig. 4 that the AUT NF truncation level depends on the frequency and the field truncation is more visible in the plane cut $z_{meas} = 0$ than the plane cut $y_{meas} = 0$. Hence, the calculated far-field (from NF to FF transformation) is damaged by the truncation error in the cut plane $\theta = \pi/2$ more than the cut plane $\phi = 0$. Let us recall that the angular area of the free error FF is for $30deg \leq \theta \leq 150deg$ and $-68deg \leq \phi \leq 68deg$.

In Figs. 7, we present the FD FFs comparison at the plane cut $\phi = 0$. The FF for high and low frequencies of $F_{-\chi dB}$ fits well the actual far-field when the sampling criterion reaches the Nyquist limit ($\lambda/2$) for $30deg \leq \theta \leq 150deg$. Also, the FF results for $30deg \leq \theta \leq 150deg$ are identical using $\chi = 1.3$ and $\chi = 1.5$ even for the frequency $2.8GHz$. In Figs. 8, we compare the calculated FFs with the actual one in the plane cut $\theta = \pi/2$. As shown, the results are more sensitive to the truncation error compared with the results of Figs. 7. The FFs for $\chi = 1.3, 1.4$ and 1.5 are similar for $-40deg \leq \phi \leq 40deg$. The measured NF amplitude at the edge of the measurement surface is only $-22.6dB$ lower than the maximum NF amplitude in the plane cut $z_{meas} = 0$. Consequently, the FF for $-68deg \leq \phi \leq -40$ and $40deg \leq \phi \leq 68$ presents important errors.

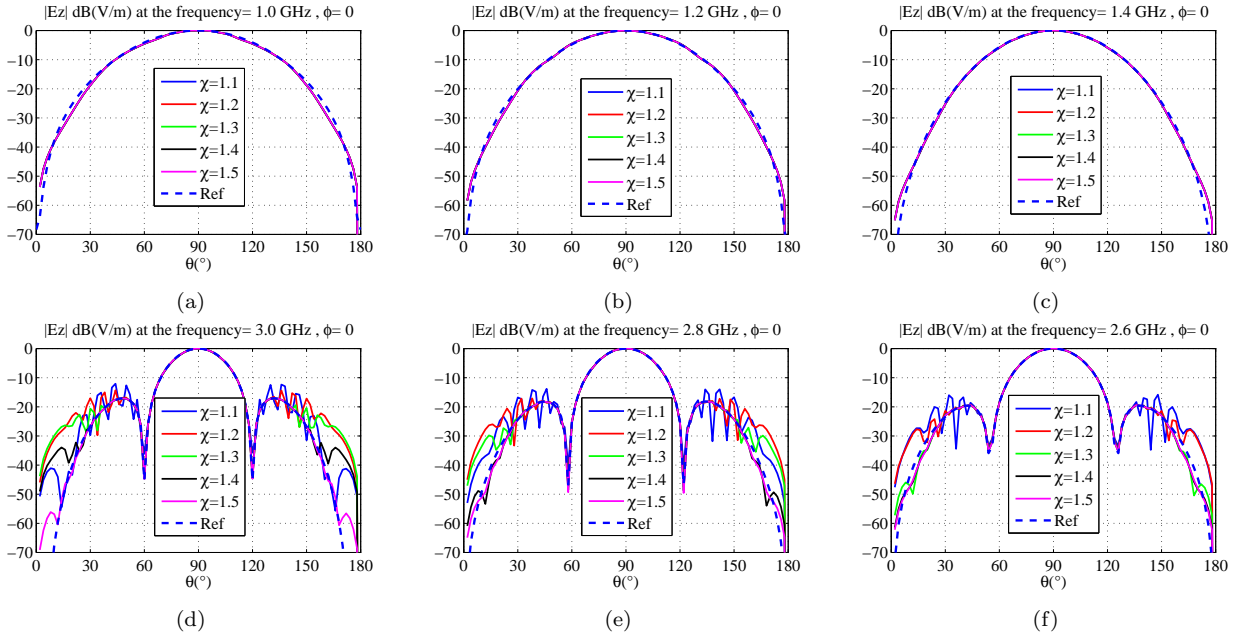


Figure 7: Comparison of far-field E_z -component at the plane cut $\phi = 0$ with $D_{max} = 150cm$, $x_{meas} = 50cm$ and $\Delta y = \Delta z = \lambda_0/2\chi$ for $\chi = 1.1, 1.2, 1.3, 1.4, 1.5$. (a-d) For $1GHz$ and $3GHz$ (F_{-30dB}) respectively. (b-e) For $1.2GHz$ and $2.8GHz$ (F_{-20dB}) respectively. (c-f) For $1.4GHz$ and $2.6GHz$ (F_{-10dB}) respectively.

When the truncation level of the AUT NF measurement data changes significantly as a function of the frequency, the measurement surface has to be adapted to satisfy the same truncation level for every frequency. Otherwise, if the measurement surface stays unchanged, the AUT valuable measurement frequency band is chosen as a function of the truncation level of the measured field. In particular, when measuring the NF of the AUT in the time-domain, we can primarily verify by measuring in the principal cut planes $y_{meas} = 0$ and $z_{meas} = 0$ the level of the E-field truncation level for every measured frequency by Fourier transforming the time-domain NF. Then, we calculate the NF truncation level by determining the level difference between the maximum E-field and the field level at the measurement surface limit for each frequency. The AUT presents at the cut plane $z_{meas} = 0$ the truncation levels of $(22.58dB, 26, 18dB)$, $(33.84dB, 24.40dB)$, $(28.78dB, 33.35dB)$ and $(27dB, 26.45dB)$ for F_{-30dB} ($1GHz$ and $3GHz$), F_{-20dB} ($1.2GHz$ and $2.8GHz$), F_{-10dB} ($1.4GHz$ and $2.6GHz$) and F_{-3dB} ($1.7GHz$ and $2.3GHz$), respectively as presented in Fig. 9.

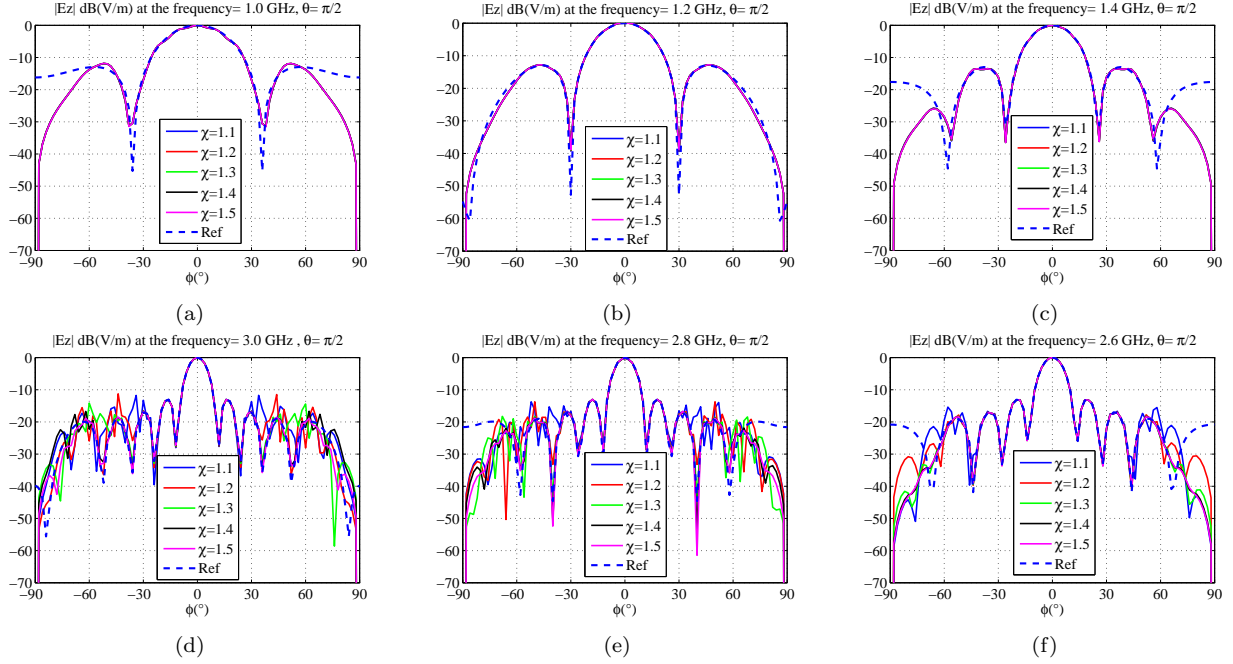


Figure 8: Comparison of far-field E_z -component at the plane cut $\theta = \pi/2$ with $D_{max} = 150cm$, $x_{meas} = 50cm$ and $\Delta y = \Delta z = \lambda_0/2\chi$ for $\chi = 1.1, 1.2, 1.3, 1.4, 1.5$. (a-d) For $1GHz$ and $3GHz$ (F_{-30dB}) respectively. (b-e) For $1.2GHz$ and $2.8GHz$ (F_{-20dB}) respectively. (c-f) For $1.4GHz$ and $2.6GHz$ (F_{-10dB}) respectively.

The AUT NF measurement data guarantee truncation levels less than $-30dB$ in the plane cut $y_{meas} = 0$. As a consequence, the far-field is accurately calculated at the plane cut $\phi = 0$ for $30deg \leq \theta \leq 150deg$. The NF plane cut $y_{meas} = 0$ presented in Fig. 9 (b) shows truncation levels of $-22.5dB$ for $1GHz$ ($\chi = 1.5$) and $24.4dB$ for $2.8GHz$ ($\chi = 1.4$) which are responsible of the FF discrepancies in frequency and time domains. From Fig. 9 (b), the frequency $2.6GHz$ ($\chi = 1.3$) is the highest frequency allowing the lowest truncation error level. For this reason the errors presented in the time-domain in Fig. 5-6-7 for $\chi = 1.3$ were equivalent to the error associated with $\chi = 1.5$. For this AUT and this measurement surface ($D_{max} = 150cm$), the maximum frequency to consider for the time-domain NF sampling criterion is $2.6GHz$ ($\chi = 1.3$). The FD FF results confirm these conclusions.

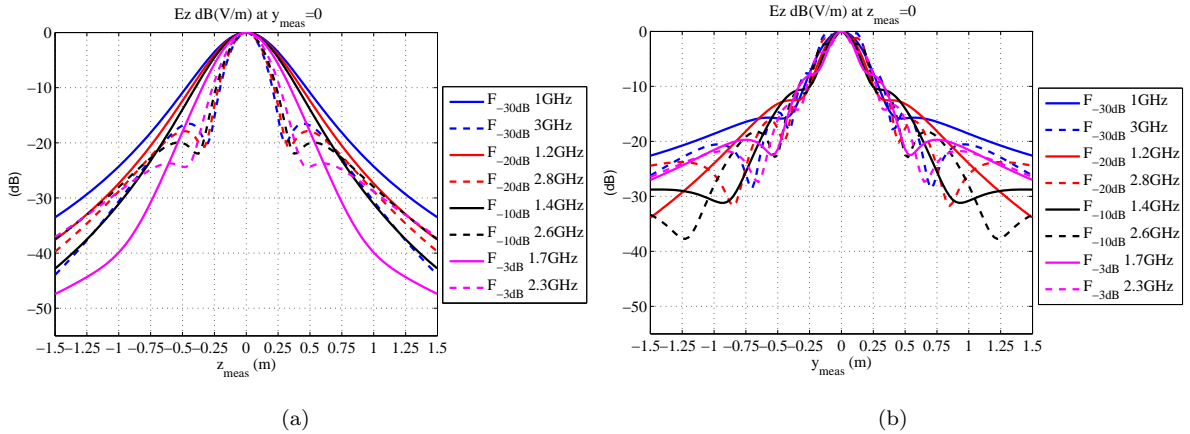


Figure 9: The normalized E_z NF component for F_{-30dB} ($3GHz, 1GHz$), F_{-20dB} ($2.8GHz, 1.2GHz$), F_{-10dB} ($2.6GHz, 1.4GHz$), F_{-3dB} ($2.3GHz, 1.7GHz$). (a) At the plane cut $y_{meas} = 0$. (b) At the plane cut $z_{meas} = 0$.

3.2. The near-field measurement distance and the sampling criterion

3.2.1. The time-domain far-field results comparison

Let us consider the NF measurement surface with $D_{max} = 150cm = 10\lambda_0$. We are interested in studying the effect of the NF measurement distances x_{meas} where the TD NF data are collected with $\Delta y_\chi = \Delta z_\chi = \lambda_0/3$ ($\chi = 1.5$). The actual TD FF is compared with the ones calculated using the TD NF to FF transformation for different measurement distances $x_{meas} = 10cm$ ($2\lambda_0/3$), $20cm$ ($4\lambda_0/3$), $30cm$ ($2\lambda_0$), $40cm$ ($8\lambda_0/3$) and $50cm$ ($10\lambda_0/3$). The errors resulting from these comparisons are presented in Fig. 10 (a) and (b) for the directions $(\theta = \pi/2, \phi = 0)$ and $(\theta = \pi/3, \phi = 0)$ respectively. As it is seen in Fig. 10(a-b), the error depends on the measurement distance, especially for $4ns \leq t \leq 6ns$. The error values decrease as the measurement distance increases.

Namely, it is difficult to set the limit of the radiating NF zone (Fresnel zone) in the TD NF measurement. The Fresnel zone is defined based on the AUT size and the operating frequency. In TD NF measurement we deal with a frequency band and the NF data measured below the Fresnel zone contain evanescent modes that are probably responsible of the errors for $4ns \leq t \leq 6ns$. Considering smaller antennas, the Fresnel zone is rapidly reached and the errors for $4ns \leq t \leq 6ns$ are smaller because less evanescent NF modes are taken into account. In [10] authors have considered a point source and the Fresnel zone is rapidly reached (low evanescent mode) for that case. This explains the early-time far-field free from truncation error as presented in [10].

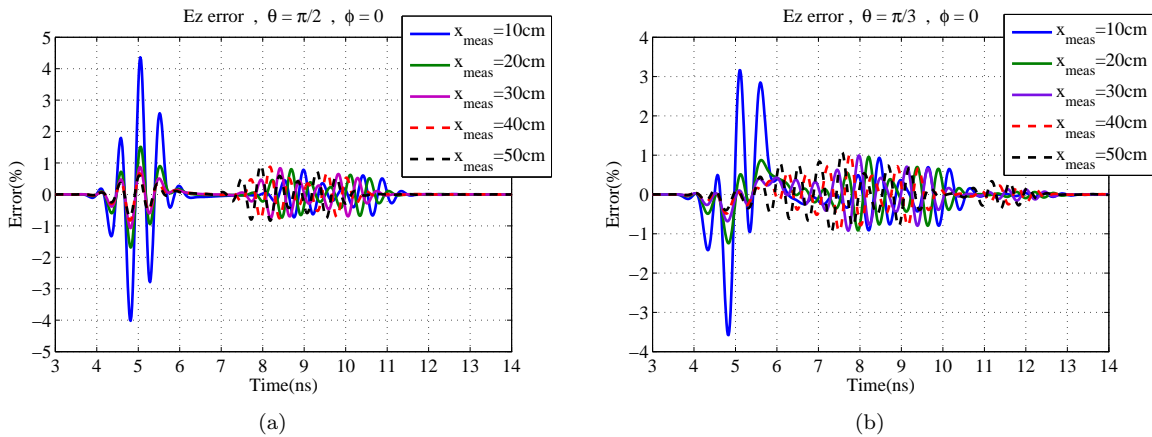


Figure 10: The Ez error as a function of time and as a function of the NF measurement distance (x_{meas}) for the FF observation points (a) $\theta = \pi/2$ and $\phi = 0$, (b) $\theta = \pi/3$ and $\phi = 0$.

In addition, from Fig. 10(a), we can isolate the effect of the measurement distance error ($4ns \leq t \leq 6ns$) since the truncation error happens later in time and the same error level is observed for every measurement distance for $7ns \leq t \leq 11ns$. If the measurement distance is larger than $2\lambda_0$ ($30cm$), the error values for $x_{meas} = 2\lambda_0$ are equivalent to the error values for $x_{meas} = 50cm$. In contrast with Fig. 10(b), it is difficult to distinguish between the measurement distance error and the truncation error.

3.2.2. The frequency-domain far-field results comparison

We are interested in studying in frequency-domain the effect of the measurement distance x_{meas} . The FF results presented in Fig. 11 are determined by Fourier transforming the time-domain results of the NF to FF transformation of NF data collected at $x_{meas} = 10cm, 20cm, 30cm, 40cm$ and $50cm$ with the sampling criterion $\Delta y_\chi = \Delta z_\chi = \lambda_0/3$ ($\chi = 1.5$). The comparisons presented in Fig. 10 show that TD FF errors decrease as the measurement distance increases. The time-domain errors are helpless to identify which frequency is mostly sensitive to the measurement distance. In contrast, the FD comparisons presented in Fig. 11 (a-d) show that the frequency ($1GHz$) is sensitive to the measurement distance with a maximum difference of $1.47dB$ at $\phi = 0$ and $1.45dB$ at $\theta = \pi/2$. The frequency $1.2GHz$

presented in Fig. 11 (b-e) shows a maximum difference of $0.4dB$. The other frequencies (greater than $1.4GHz$) stay unchanged ($error \leq 0.2dB$) since the NF measurement distance is greater than a wavelength.

As a conclusion, using $D_{max} = 150cm$ and $x_{meas} \geq 2\lambda_0$ the error values are of the same order for $\chi = 1.3$ and $\chi = 1.5$. Hence, $F_{-10dB} \approx 1.3f_0$ can be considered as the maximum frequency for NF sampling of this AUT. We have tried to isolate the effect of three important measurement parameters in the planar TD NF technique. These parameters are : the measurement distance (reactive NF), the surface truncation (truncation error) and the NF sampling criterion (aliasing error). As it is presented in Figs. 5-6-7 it is difficult to predict from TD FF errors the consequences over the AUT radiation pattern in the frequency-domain. For this reason, the frequency-domain (FD) comparisons have been presented to make out the effect of each parameter over the AUT FD FF.

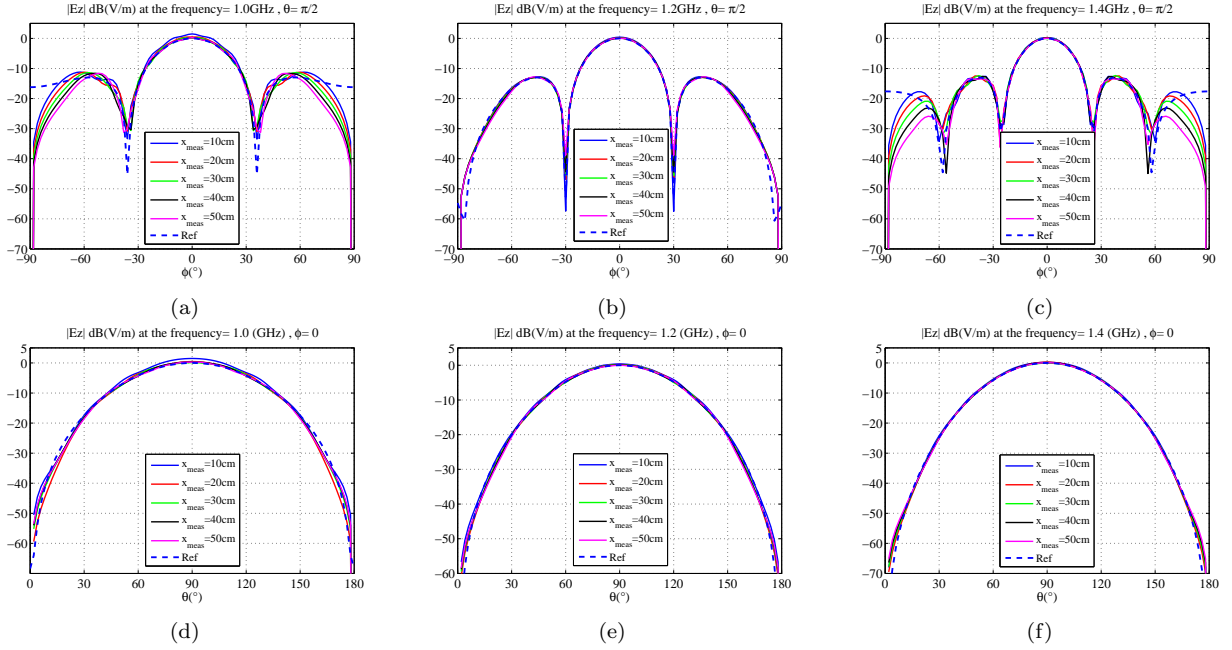


Figure 11: Comparison of the FF radiation pattern for $x_{meas} = 10cm, 20cm, 30cm, 40cm$ and $50cm$ at the plane cut $\theta = \pi/2$, (a) at $1GHz$, (b) at $1.2GHz$, (c) at $1.4GHz$. Comparison of the FF radiation pattern at the plane cut $\phi = 0$, (d) at $1GHz$, (e) at $1.2GHz$, (f) at $1.4GHz$.

4. CONCLUSION

The effect of three parameters in planar time-domain near-field to far-field transformation have been presented. The followed approach aims to optimize the computation time and memory requirements by studying the near-field sampling measurement criterion. For antennas characterization using the time-domain near-field technique, we have shown that multiple conditions have to be met to correctly calculate the far-field. The size of the measurement surface decides predominantly on the frequency band to consider. The NF spatial truncation is responsible for the frequency limitation. The maximum frequency taken into account depends on the antenna excitation pulse and the behaviour of the AUT near-field *directivity* as a function of the frequency. Once the maximum frequency is defined, the sampling criterion is based on the Nyquist rate. Specific care has to be applied in choosing the measurement distance which determine the minimum frequency to be considered. Comparisons in TD and FD have been carried out to confirm these assumptions.

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