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Model Predictive Control with Two-step horizon for Three-level Neutral-Point Clamped inverter

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Abstract—This paper presents a detailed description of Finite Control Set Model Predictive Control (FCS-MPC) applied to three-level neutral point clamped inverter (3L-NPC). The controller uses a model of the converter, DC link and load to calculate predictions of the future values of the load currents and DC-link capacitor voltages for all possible voltage vectors. The cost function is defined to minimize the error between the reference currents and predicted load currents, balance the DC-link capacitor voltage and reduce the switching frequency. The optimal switching state that minimizes the cost function is selected and applied to the converter. Furthermore, the quality of the current and voltage are improved by using a two prediction steps procedure. Simulation results for the one and two prediction step are presented and compared with linear current controller and space-vector modulation (PI-SVM). The obtained results show the better performances of the proposed control method.

I. INTRODUCTION

In recent years, many industrial applications began demanding high power converters such as new energy systems, high voltage direct current transmission, especially with the development of high power generators using wind power (with the medium voltage and high power level of more than 1 MW). With the development of power electronics, many new multi-level converters have been proposed: diode-clamped (neutral-clamped), flying capacitor and cascaded H-bridge. Among them, three-level neutral point-clamped inverter structure is considered a good solution due to its advantages: reduce the total harmonic distortion (THD), common mode voltage, increase the capacity of the inverter thanks to a decreased voltage applied to each component [1], [3], [4].

Predictive control for power converters and electric drives is a modern control method that has a big potential for application in the power conversion system. Among the advanced control technology, the Model Predictive Control (MPC) is one that has been successfully used in industrial applications because it has several advantages, such as easy inclusion of non-linearities in the model, constraint and delay compensation. Since the converter has a finite number of switching states, in this case, the control method is known as a finite control set model predictive control (FCS-MPC).

This article proposes an improved FCS-MPC to control the load current for 3L-NPC while maintaining the balance between the DC link capacitor voltage and reducing the switching frequency. These objectives are accomplished through the cost function. First, the discrete-time model of the three-level inverter is established, and then the predicted values of the outputs (current, DC capacitor voltages) for the control variable corresponding to all switching state are estimated. Finally, the optimal switching state with the minimum cost function is selected and applied to the inverter. However, this method has one problem: it needs a high amount of calculations. This makes the calculation time considerable, and increases the delay between the measurements and the actuation. In order to compensate this delay, reduce the amount of calculation and improve the quality of the current, the method proposed in the present paper uses two-step prediction with same voltage vector during two steps, instead of different vectors. A comparison between MPC with one and two-step prediction and PI-SVM for different conditions of references and loads using Matlab/Simulink verify the correctness and feasibility of the proposed method.

This paper is organized as follow: section 2 presents the mathematical model of the three-level inverter. Section 3 explains the proposed control method. In section 4, simulation results are represented and analyzed and finally section 5 draws the conclusion.

II. MODEL OF THREE-LEVEL NEUTRAL POINT CLAMPED INVERTER

A. Topology

Figure 1 shows a simplified diagram of the three-level neutral point clamped inverter. Each inverter branch is composed of four switches with four anti-parallel diodes. On the DC side of the converter, the DC bus capacitor is divided into two parts, by providing a neutral point Z [1], [3]. The diodes are connected to the neutral point Z, $D_{Z_{11}}$ and $D_{Z_{12}}$ are clamping diodes. The voltage across each of the DC capacitor is normally equal to the half of the total DC voltage $U_{dc}$. The operating status of 3L-NPC switches can be represented by three switching states [P], [O] and [N]. The switching state [P] or [1] signifies both $S_{11}$ and $S_{12}$ switches in branch A are states "ON" and the inverter terminal voltage $U_{AZ}$ has the value $+U_{dc}/2$, while [N] or [-1] indicates two switches $S_{13}$ and $S_{14}$ are conditions "OFF", leading to $U_{AZ} = -U_{dc}/2$. The switching state [O] or [0] means that the two internal switches $S_{11}$ is "ON" state and $S_{12}$ is "ON" and $U_{AZ}$ is clamped to zero through the clamping diodes. Taking into account the three phases of the inverter, there are in total 27 possible combinations of switching states corresponding to 19 voltage vectors. Considering the voltage vector definition for the output voltage:

$$u_s = \frac{2}{3}(u_{AZ} + u_{BZ} + a^2 u_{CZ}) \quad (1)$$
with \( a = e^{j2\pi/3} = -\frac{1}{2} + j\frac{\sqrt{3}}{2} \)

**B. Mathematical model**

In order to ensure proper operation of the inverter, the two voltages across the capacitors must be maintained equal to half of the total voltage:

\[
u_{C1} = u_{C2} = U_{dc}/2\tag{2}\]

To clarify the operation of the three-phase inverter, we took the first switching branch (table I) as an example: \( u_1 \) is the voltage between the midpoint of the branch and negative voltage. From the analysis, we can express the voltage as follows:

\[
u_1 = \sum_{i=1}^{2} S_{ii} u_i C_i = S_{11} u_{C1} + S_{12} u_{C2}\tag{3}\]

From equation (3), we can express three-phase voltages set in matrix form as below:

\[
\begin{bmatrix}
  u_1 \\
  u_2 \\
  u_3
\end{bmatrix} =
\begin{bmatrix}
  S_{11} & S_{12} \\
  S_{21} & S_{22} \\
  S_{31} & S_{32}
\end{bmatrix}
\begin{bmatrix}
  u_{C1} \\
  u_{C2}
\end{bmatrix}
\tag{4}\]

<table>
<thead>
<tr>
<th>( S_{ii} )</th>
<th>( S_{ij} )</th>
<th>( S_{kl} )</th>
<th>( u_1 )</th>
<th>( u_2 )</th>
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</thead>
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<tr>
<td>1</td>
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<td>0</td>
<td>0</td>
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<tr>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>1</td>
</tr>
</tbody>
</table>

The voltage on one phase of the load \( u_{ak} \) can be written in terms of voltage \( u_1 \) to \( u_3 \) inverter as follows:

\[
\begin{align*}
u_{s1} &= \frac{1}{3}(2u_1 - u_2 - u_3) \\
u_{s2} &= \frac{1}{3}(-u_1 + 2u_2 - u_3) \\
u_{s3} &= \frac{1}{3}(-u_1 - u_2 + 2u_3)\tag{5}\end{align*}
\]

From equations (4) and (5), the load voltages are expressed in terms of DC link capacitor voltages and switching states as follows:

\[
\begin{bmatrix}
  u_{s1} \\
  u_{s2} \\
  u_{s3}
\end{bmatrix} =
\begin{bmatrix}
  S_{C11} & S_{C12} \\
  S_{C21} & S_{C22} \\
  S_{C31} & S_{C32}
\end{bmatrix}
\begin{bmatrix}
  u_{C1} \\
  u_{C2}
\end{bmatrix}\tag{6}\]

The equation of current with load RL and electromotive force (EMF) can be written as:

\[
\begin{align*}
R_{i_s1} + L \frac{di_{s1}}{dt} + e_1 &= u_{s1} \\
\frac{di_{s1}}{dt} &= -\frac{R}{L} i_{s1} + \frac{1}{L} (u_{s1} - e_1)\tag{8}\end{align*}
\]

Or we can express three-phase currents set in matrix form as below:

\[
\frac{d}{dt}
\begin{bmatrix}
  i_{s1} \\
  i_{s2} \\
  i_{s3}
\end{bmatrix} =
\begin{bmatrix}
  -R/L & 0 & 0 & S_{C11}/L & S_{C12}/L \\
  0 & -R/L & 0 & S_{C21}/L & S_{C22}/L \\
  0 & 0 & -R/L & S_{C31}/L & S_{C32}/L
\end{bmatrix}
\begin{bmatrix}
  i_{s1} \\
  i_{s2} \\
  i_{s3}
\end{bmatrix}
\begin{bmatrix}
  u_{C1} \\
  u_{C2}
\end{bmatrix}
\begin{bmatrix}
  e_1 \\
  e_2 \\
  e_3
\end{bmatrix}\tag{9}\]

On other hand, the neutral current \( i_{dc} \) can be calculated from three-phase load currents and the switching states as follows (Fig. 1):

\[
i_{dc} = (S_{11} - S_{12})i_{s1} + (S_{21} - S_{22})i_{s2} + (S_{31} - S_{32})i_{s3} = i_{s2} - i_{s1} = H_{s1} i_{s1} + H_{s2} i_{s2} + H_{s3} i_{s3}\tag{10}\]

Where \( H_{s1} = 1 \) when \( S_{11} = 1, S_{12} = 0 \), otherwise \( H_{s1} = 0 \)

Assuming that the DC bus voltage \( U_{dc} \) is constant and \( C_{di} = C_{d2} = C \):

\[
i_{c1} = C \frac{du_{C1}}{dt} = C \frac{d(U_{dc} - u_{C2})}{dt} = -C \frac{du_{C2}}{dt} = -i_{c2}\tag{11}\]

By substituting equation (10) into equation (11), the DC-link capacitor voltages are expressed as follows:

\[
\begin{align*}
\frac{du_{C1}}{dt} &= -\frac{1}{2C}(H_{s1} i_{s1} + H_{s2} i_{s2} + H_{s3} i_{s3}) \\
\frac{du_{C2}}{dt} &= \frac{1}{2C}(H_{s1} i_{s1} + H_{s2} i_{s2} + H_{s3} i_{s3})\tag{12}\end{align*}
\]

Based on equation (9) and (12), the three-phase currents and the DC-link capacitor voltages can be expressed in matrix form.
The aim of the current control scheme is to minimize the error between the predicted current and the reference values, to maintain voltage balance of the capacitor and to reduce the switching frequency. The cost function for 3L-NPC has the following compositions [2], [4], [6]:

$$ g = (i_α - i_{α}^*)^2 + (i_β - i_{β}^*)^2 + λ_{dc}|u_{c1} - u_{c2}^*| + λ_n n_c $$  \hspace{1cm} (15)$$

Where \( i_{α}^* \) and \( i_{β}^* \) are the real and imaginary components of the predicted current; \( i_α \) and \( i_β \) are the real and imaginary components of the reference current. \( n_c \) is the number of switching change when the switching state \( S(k) \) is applied compared with previous state \( S(k-1) \). It can be expressed as follows:

$$ n_c = |S_a(k) - S_a(k-1)| + |S_b(k) - S_b(k-1)| + |S_c(k) - S_c(k-1)| $$  \hspace{1cm} (16)$$

where \( S_a \) represents the state of a switch and has three states: [-1, 0, 1].

III. THE APPLICATION OF MPC TO 3L-NPC INVERTER

The FCS-MPC controller predicts the behavior of the inverter for finite possible voltage vector on each sampling interval. A cost function is used to evaluate the voltage vector for the next sampling interval based on the prediction model. The optimal switching time is selected and applied to the inverter during the next sampling period which minimizes the cost function. The schematic MPC is shown in Fig. 2.

The aim of the current control scheme is to minimize the error between the predicted current and the reference values, to maintain voltage balance of the capacitor and to reduce the switching frequency. The cost function for 3L-NPC has the following compositions [2], [4], [6]:

$$ g = (i_α - i_{α}^*)^2 + (i_β - i_{β}^*)^2 + λ_{dc}|u_{c1} - u_{c2}^*| + λ_n n_c $$  \hspace{1cm} (15)$$

Where \( i_{α}^* \) and \( i_{β}^* \) are the real and imaginary components of the predicted current; \( i_α \) and \( i_β \) are the real and imaginary components of the reference current. \( n_c \) is the number of switching change when the switching state \( S(k) \) is applied compared with previous state \( S(k-1) \). It can be expressed as follows:

$$ n_c = |S_a(k) - S_a(k-1)| + |S_b(k) - S_b(k-1)| + |S_c(k) - S_c(k-1)| $$  \hspace{1cm} (16)$$

where \( S_a \) represents the state of a switch and has three states: [-1, 0, 1].
can be expressed as follows:
\[
\begin{align*}
    u_{C1}(k+2) &= u_{C1}(k+1) + \frac{1}{2}i_{c1}(k+1)T_s \\
    u_{C2}(k+2) &= u_{C2}(k+1) + \frac{1}{2}i_{c2}(k+1)T_s
\end{align*}
\] (23)

Where
\[
\begin{align*}
    i_{c1}(k+1) &= -\frac{1}{2}\left(H_{s1}i_{s1}(k) + H_{s2}i_{s2}(k) + H_{s3}i_{s3}(k)\right) \\
    i_{c2}(k+1) &= -\frac{1}{2}\left(H_{s1}i_{s1}(k) + H_{s2}i_{s2}(k) + H_{s3}i_{s3}(k)\right)
\end{align*}
\] (24)

Hence, the cost function of MPC for the 3L-NPC inverter with one step prediction can be expressed as:
\[
g = \left(i^*_a(k+1) - i^p_a(k+1)\right)^2 + \left(i^*_b(k+1) - i^p_b(k+1)\right)^2 \\
+ \left(i^*_c(k+2) - i^p_c(k+2)\right)^2 + \left(i^*_b(k+2) - i^p_b(k+2)\right)^2 \\
+ \lambda_{dc}\left|u_{C1}(k+1) - u_{C2}(k+1)\right| + \lambda_n n_c
\] (25)

The expression of the cost function with two-step prediction can be written as follows:
\[
g = \left(i^*_a(k+1) - i^p_a(k+1)\right)^2 + \left(i^*_b(k+1) - i^p_b(k+1)\right)^2 \\
+ \left(i^*_c(k+2) - i^p_c(k+2)\right)^2 + \left(i^*_b(k+2) - i^p_b(k+2)\right)^2 \\
+ \lambda_{dc}\left|u_{C1}(k+2) - u_{C2}(k+2)\right| + \lambda_n n_c
\] (26)

The future currents \(i^*(k+1), i^*(k+2)\) are estimated by extrapolation using Lagrange method based on the present and passed value. This process can be expressed as follows:
\[
\begin{align*}
i^*(k+1) &= 3i^*_a(k+1) - 3i^*_a(k-1) + i^*_b(k-2) \\
i^*(k+2) &= 6i^*_a(k+1) - 8i^*_a(k-1) + 3i^*_b(k-2)
\end{align*}
\] (27)

IV. SIMULATION RESULTS

To evaluate the quality performance, we can use the mean square error (MSE). It can be express as follows:
\[
MSE = \frac{1}{n}\sum_{i=1}^{n}\left(y_i - y^p_i\right)^2
\] (28)

where \(y^*_i\) is the reference vector and \(y^p_i\) is the vector of prediction.

On other hand, in order to estimate the average switching frequency per semiconductor \(f_{sw}\) of FCS-MPC, the following expression can be used [2], [4]:
\[
f_{sw} = \sum_{i=1}^{4}\frac{f_{swi} + f_{sw1} + f_{sw3}}{12}
\] (29)

where \(f_{swi}\) is the average switching frequency during a time interval of power switching number i of phase k, with i \(\in\) \{1, 2, 3, 4\} and k \(\in\) \{a, b, c\}.

The proposed predictive control is analyzed and compared with linear current controller and space vector modulation (PI-SVM). The parameters of inverter is summarized in table II.

To generate the same average switching frequency per semiconductor, the sampling frequency of the FCS-MPC is considered \(f_s = 10kHz\) and the sampling frequency of the SVM is 5 kHz. For the SVM at 5 kHz, \(f_{sw} = 2.5kHz\) and
the expected value of $f_{sw}$ for FCS-MPC is about 2.5 kHz. The transient responses of the PI-SVM and MPC from zero load current until the steady state and the total harmonic distortion (THD) are illustrated in Fig. 5 and Fig. 6. In order to observe the dynamics ability to track the current reference and the interaction between two components of the load current, the amplitude of the current reference steps from 10 A to 5 A (Fig. 7(a)), then steps from 5 A to 10 A (Fig. 7(b)) at \( t = 0.065 \text{[s]} \). The mean square error of PI-SVM is 0.336 and 0.097 with MPC. From the results presented, it is clear that the predictive method obtains an accurate current tracking ability with a low THD and low current ripple. In addition, it has a fast dynamic response (the corresponding computation time of the algorithm were 0.07msec) with inherent decoupling between two components: real and imaginary (Fig. 8).

One of the important issues of 3L-NPC structure is the balancing voltage of the DC-link capacitor. It is obvious that the voltage of DC-link capacitor remains balanced in spite of the transition of the current reference (Fig. 9).

To compare a MPC with one-step with two-step proposed, we can analyze the characteristic with the load RL with weighting value $\lambda_{dc} = 0.45$ and $\lambda_{n} = 0.001$ in equation

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Description</th>
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</thead>
<tbody>
<tr>
<td>$U_{dc}$</td>
<td>540 [V]</td>
<td>DC-link voltage</td>
</tr>
<tr>
<td>C</td>
<td>1 [mF]</td>
<td>DC-link capacitor</td>
</tr>
<tr>
<td>R</td>
<td>10 [Ω]</td>
<td>Load resistance</td>
</tr>
<tr>
<td>L</td>
<td>50 [mH]</td>
<td>Load inductance</td>
</tr>
<tr>
<td>$f_s$</td>
<td>10 [kHz]</td>
<td>Sampling frequency for FCS-MPC</td>
</tr>
<tr>
<td>$f_{svm}$</td>
<td>5 [kHz]</td>
<td>Sampling frequency for PI-SVM</td>
</tr>
<tr>
<td>f</td>
<td>50 [Hz]</td>
<td>Current reference frequency</td>
</tr>
<tr>
<td>E</td>
<td>100 [V]</td>
<td>Back-EMF peak amplitude</td>
</tr>
<tr>
<td>$I_{e,f}$</td>
<td>10 [A]</td>
<td>Peak amplitude of reference current</td>
</tr>
</tbody>
</table>

Fig. 5. The transient response and THD of three-phase current for PI-SVM

Fig. 6. The transient response and THD of three-phase current for FCS-MPC

Fig. 7. The load current transient response for a reference step of 10A-5A

Fig. 8. The load current response for a reference step of 5A-10A
The load current with one-step prediction, which is illustrated in Fig. 10, creates 1.48% THD. The average switching frequency $f_{sw}$ is 1280 Hz. The load current with two-step prediction, which is shown in Fig. 11, creates 1.21% THD, and respectively 883 Hz. Hence, this method provides a new approach to control high power converter that require an operation with lower switching frequency. Furthermore, the THD of the voltage of proposed method (26.39%) is smaller than MPC with one-step prediction (28.01%). The operating condition discussed is repeated with unbalanced load ($R_a = 12\Omega$, $R_b = 10\Omega$, $R_c = 8\Omega$). Fig. 13 shows that the load currents effectively follow their references with the unbalancing load.

V. Conclusions

This study proposes an FCS-MPC strategy with one and two steps prediction for 3L-NPC inverter. First, the mathematical model of 3L-NPC inverter is established, and then the cost function, which contains the current error, the capacitor voltage balancing and the reduction of the switching frequency, is established. In this paper, there is a comparison between PI-SVM and FCS-MPC for 3L-NPC inverter. The simulation results show that the algorithm can successfully maintain their balanced capacitor voltages and reduce the switching frequency. In addition, by using proposed method we can reduce the switching frequency and high number of calculations while maintaining an acceptable quality of current and voltage. The control strategy also allows compensating the delay time and the change of load parameters, while the load current continues effective tracking to their references. The linear PI controllers and the modulation block are further eliminated. Therefore, the proposed method is an interesting alternative to control the 3L-NPC converter.

REFERENCES