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INVESTIGATION OF IN-FLIGHT PARTICLE CHARACTERISTICS AND MICROSTRUCTURAL EFFECTS ON OPTICAL PROPERTIES OF YSZ PLASMA-SPRAYED COATINGS

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Abstract

The purpose of this study is to investigate the microstructural effects of yttria-stabilized zirconia (YSZ) plasma-sprayed coatings on their optical properties in order to improve the thermal performance of these coatings that are often used as thermal barrier coatings (TBCs). Four coatings with significant microstructural differences have been manufactured. A preliminary investigation of in-flight particle characteristics has been performed to select the spray conditions. This investigation used two complementary particle diagnostic tools: the DPV2000 system and a particle collection device. Both hemispherical transmittance and reflectance spectra of the coatings have been investigated over the 0.25-10 μ m wavelength range. The Gouesbet-Maheu four-flux model has been implemented to calculate the absorption and scattering coefficients. Their variations are discussed in terms of microstructural effects.

Keywords: Plasma spraying; In-flight particle diagnostics; Transmittance; Scattering and absorption coefficients.

Introduction

Atmospheric plasma spraying (APS) is widely used to produce ceramic thermal barrier coatings (TBCs). A TBC is a dual-layered system: the top ceramic layer, commonly yttria-stabilized or partially stabilized zirconia (YSZ), provides thermal insulation to engine components while the bond coat (NiCrAlY) increases the oxidation resistance and adapts the difference in expansion coefficient between the top coat and the substrate. Understanding the link between the processing parameters, resulting microstructural features and macroscopic properties is the key to ensure better TBC performances. Accordingly, the radiative properties of YSZ plasma-sprayed coatings must be investigated since the radiative transfer is the major

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heat transfer process at service temperatures [1]. This work is intended to establish relationships between the microstructural features of YSZ plasma-sprayed coatings and their radiative properties.

The first section describes the experimental procedure. It includes: (1) the particle in-flight monitoring with the DPV2000 system and a particle collection device to engineer coatings with microstructural differences; (2) a thorough characterization of the resulting coatings to provide a global description of the microstructural features; (3) the reflectance and transmittance measurements over the 0.25-10 μm wavelength range on annealed samples in oxidizing atmosphere at 500 $^{\circ}\text{C}$ for 24h. The second section presents the experimental results and discusses the microstructure in relation to the in-flight diagnostic results. Finally, the last section analyses the potential of the four-flux model to investigate the correlations between microstructure and radiative properties.

Experimental procedure

Materials and plasma spraying equipment

The sprayed powder is a commercial 7%-wt Y_2O_3 partially-stabilized ZrO_2 powder (Amperit 827.054 from H.C Stark) with a 10-45 μm particle size distribution. The feedstock manufacturing process is spray drying, agglomeration and sintering. It results in globular and porous particles as shown in Fig. 1.

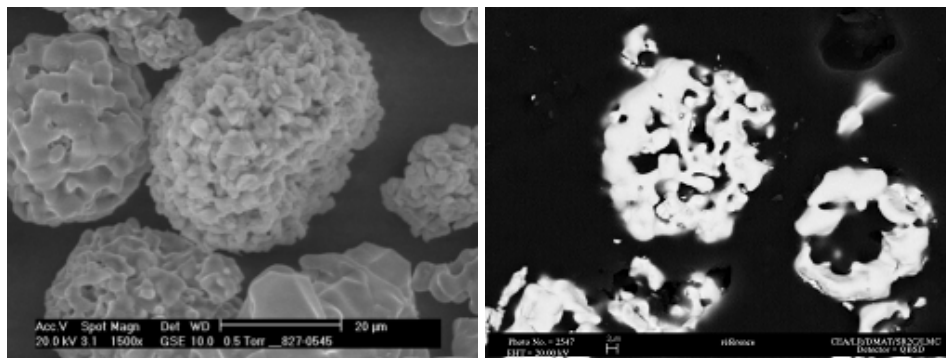


Figure 1: Morphology and cross section of ZrO_2 -7wt.% Y_2O_3 particles

A X13M stainless steel grade (Aubert&Duval, France) has been selected as substrate material in order to minimize the expansion mismatch stress during the coating formation as its expansion coefficient α is very close to that of YSZ: at 25 $^{\circ}\text{C}$, $\alpha_{\text{X13M}}=10.6 \times 10^{-6} \text{ }^{\circ}\text{C}^{-1}$ and $\alpha_{\text{YSZ}}=10.5 \times 10^{-6} \text{ }^{\circ}\text{C}^{-1}$. The disk-shape substrates (25mm in diameter and 5mm in thickness) have been grit-blasted to $\text{Ra}=4\mu\text{m}$ and disposed on a cylindrical holder (160mm in diameter) at a stand-off distance of 120mm from the spray gun nozzle exit.

Plasma-sprayed 500 μ m-thick coatings have been manufactured with a F4-VB torch (Sulzer Metco AG, Switzerland). The powder has been injected through a 1.5-mm internal diameter injector perpendicular to the plasma torch axis and located at 6 mm from the nozzle exit. The powder carrier gas has been adjusted in such a way that the median trajectory of the spray jet made an angle of 3.5° with the torch axis. During spraying, the substrate and coating surface temperature, monitored continuously with an Ircon pyrometer ($8 < \lambda < 14 \mu\text{m}$, 10Hz), has been adjusted at 200°C (transition temperature) by an argon cryogenic cooling system. Below this temperature value, the impacting droplets splatter into several interconnected fragments while above, the droplets retain their coherence and spread out in the form of disks [2]. In addition, this temperature makes it possible to restrict the substrate oxidation during the preheating stage.

To engineer coatings with significant microstructural differences, the following operating parameters have been varied: torch nozzle internal diameter (6 or 8 mm), arc current (320 to 600 A), gas mixture composition (binary or ternary mixtures of argon, hydrogen and helium) and gas flow rates. The spray conditions have been selected by using particle diagnostic tools to obtain a large range of in-flight particle characteristics.

Particle diagnostic tools

Particle in-flight diagnostics have been performed, at the stand-off distance (120mm) without the substrate, using a DPV2000 system and a device to collect the in-flight particles.

The Tecnar DPV2000 system provides temperature and velocity distributions by collecting the thermal radiation emitted by hot particles with an optical sensing head. The temperature is determined by using a two-color fast pyrometer working at $\lambda_1=792\mu\text{m}$ and $\lambda_2=1004\mu\text{m}$ and assuming that the material behaves as a grey body [3]. However, at these two wavelength values, YSZ is reported to be translucent at high temperature [1] and thermal gradients could exist within particles. Besides, the DPV2000 system records signal issued from hot particles emitted fluxes that means that overheated small particles and larger ones at a temperature lower by hundreds of K can give the same thermal radiation due to their surface ratio. Therefore, in this paper, the measured temperatures are not absolute values. However, the trends they give allows the comparison of the spray conditions.

An in-flight particle collecting system has been designed in order to study the melting state of particles when they impact on the substrate. It consists of four main parts: a stainless steel barrel (100mm in internal diameter and 200mm in length) with four 12.5mm-sized blowholes,

a copper water-cooled upper part with a 25mm-sized hole, a protective stainless steel top diaphragm and a copper bottom part with two argon cryogenic nozzles. The liquid argon tank pressure and the argon atomizing gas pressure have been adjusted according to the spray conditions in order to quench the sprayed powder. The whole has been positioned horizontally at 120mm from the nozzle exit and aligned with the center of the sprayed spot.

After collection, scanning electronic microscopy (SEM) observations of particle cross sections have been performed and a digital image analysis routine has been implemented to evaluate the melting state of the collected particles. Since a good heat treatment of particles in the plasma jet usually results in denser spheroidized particles, the morphology of the particles and their internal porosity content have been studied to quantify the melting state. Two magnifications x50 and x250 have been chosen to evaluate these criteria. The morphological analysis has been performed on a 1600- μm x 1200- μm field of view which includes 1000-2000 particles on average. This enables a proper statistical analysis. The porosity determination has been performed using a 320- μm x 240- μm field of view. Before analysis, the micrographs have been treated by a software to discard the particles in contact with the image edges, separate the agglomerated particles and remove the particle splinters due to the metallographic preparation.

Microstructural analysis of the coatings

The coating microstructure has been observed by using optical microscopy (OM) and scanning electronic microscopy (SEM) while the porous and crack network has been characterized by the combination of three techniques :

- (1) Archimedes Porosimetry that provides the open porosity level P_o .
- (2) Mercury Intrusion Porosimetry (MIP) that gives the open porosity level and pore size distribution. The measurable pore size ranges between 100 μm and a few nanometers by applying pressure from 0.1 up to 400 MPa (Micrometrics Autopore III 9410).
- (3) Image Analysis (Clemex Vision Software) that is performed on ten successive fields of view of 3.5 mm² with an optical microscope (Nikon Microphot Fxa). However, this technique cannot measure submicronic pores due to the resolution of the objective lens.

For volumetric methods (1) and (2) used to characterize the open porosity, free-standing samples have been prepared by removing the coatings from the stainless substrates by using acidic dissolution.

Annealing

A previous study [4] has demonstrated that the oxygen loss in the YSZ material during the deposition process has a strong effect on the resulting optical properties. To reduce this effect, all samples have been annealed in air at 500°C for 24h before.

Optical characterization tools

The reflectance and transmittance measurements of the plasma-sprayed free-standing coatings have been performed over the 0.25-10- μm wavelength range by means of two spectrometers: a Varian Cary 5000 spectrometer for the 0.25-2.5- μm wavelength range and a Mid-IR Bruker IF66v/s spectrometer for the 1.5-10- μm range.

Since the plasma-sprayed coatings exhibit highly scattering features [5], integrating spheres with a reflecting inner coating have been mounted to collect the hemispherical flux. Data acquisition has been performed under soft vacuum (<2000Pa) to avoid, as much as possible, the absorption bands of H₂O and CO₂.

The data measured with the Bruker spectrometer have been adjusted and merged with the Varian data between 1.5 to 2.5 μm by using the dedicated OPUS software (Bruker Optik GmbH) in order to examine the spectra over the entire wavelength range.

Results and discussion

Particle diagnostics and spray conditions

The DPV2000 monitoring made it possible to select 4 sets of spray conditions among 25 sets. The selected spray conditions and corresponding particle in-flight parameters are summarized in Table 1. The reported data correspond to the mean velocity and temperature values calculated from more than 1000 individual particles recorded in the plasma jet where the maximum particle flux is detected. Therefore, the standard deviation values encompass variations due to the particle size distribution, process instabilities (powder feeding and plasma jet fluctuations) and measurement errors.

Table 1 : Spraying conditions and corresponding in-flight particle characteristics

Condition set number	Plasma gas flow rates (slpm) Ar/He/H ₂	Total gas flow rate (x10 ⁻⁴ kg/s)	Arc current (A)	Specific enthalpy (MJ/kg)	Nozzle diameter (mm)	Particle in-flight parameters	
						T (°C)	V (m.s ⁻¹)
1	45/0/15	1.359	600	19.5	6	3014±185	280±60
2	65/30/5	2.027	550	10.7	6	2767±210	300±70
3	12/45/3	0.495	450	24.0	6	2730±130	150±25
4	6/12/1.5	0.226	450	14.2	8	2800±105	50±10

The spray conditions 1 & 2 provide high particle velocity range (280-300m/s) due to high gas flow rate, high current intensity (550-600A) and a 6mm-diameter nozzle. Conversely, the lower particle velocity values have been achieved by decreasing both the plasma gas flow rate and the arc current intensity for the spray condition 3, and also by increasing the internal diameter nozzle (8mm) for the spray condition 4.

Regarding the mean particle temperature, the selected spray conditions can be subdivided into two groups: a high temperature group (condition 1) and a “melting-point” group (conditions 2-3-4) with a temperature range close to the YSZ melting temperature (2750°C). As already mentioned, these absolute values are not meaningful to quantify the melting state of particles which depends on their dwelling time in the plasma jet and plasma-particle heat transfer.

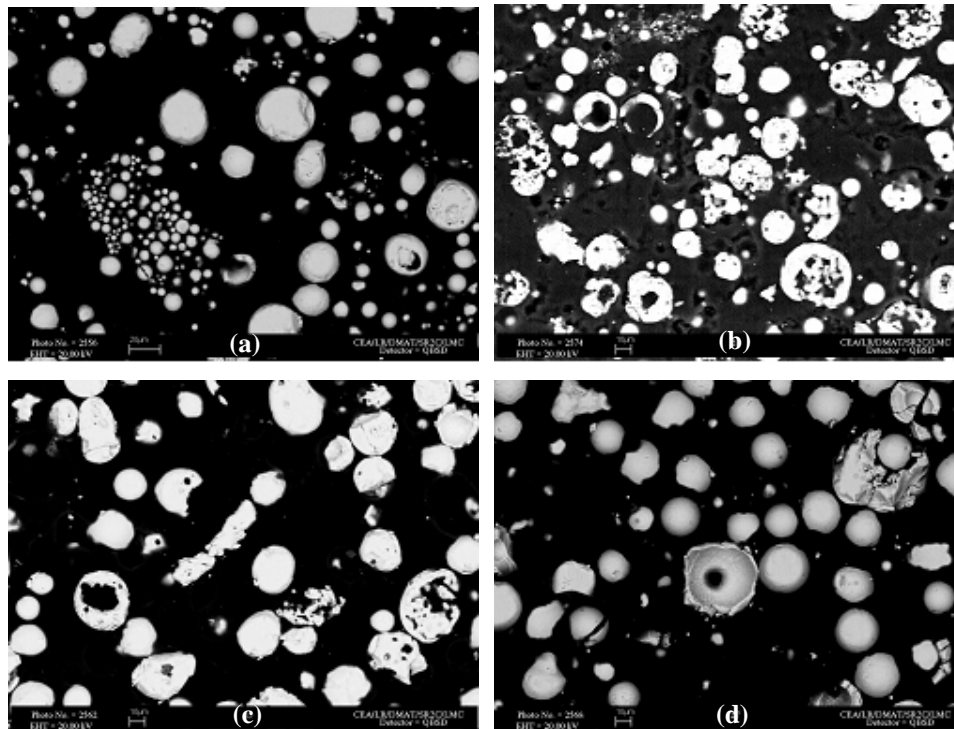
SEM cross sections of original and collected powders are shown in Fig.1 and Fig.2, respectively. It can be seen that depending on the spray conditions, the argon-quenched particles differ both in shape and internal porosity content which illustrate different melting degrees. A digital analysis method was used to perform some statistical analysis (Table 2) of the morphology and internal porosity of particles after their heat treatment in the plasma jet. The internal porosity features have been determined on the micrographs of Fig. 2 while the mean shape factor SF ($SF=4\pi A/P^2$ with A the particle area and P its perimeter) has been measured over about 1000 particles on larger field images, not reported in this paper.

Table 2 : Digital image analysis of SEM particle cross-section observations

Powder sample number	Shape Factor $0 < SF < 1$	Relative porous area per particle (%)	Mean size of internal pores (μm)
Original powder	0.92±0.14	7.4	1.54
1	0.97±0.08	2.2	0.60
2	0.89±0.16	7.1	1.08
3	0.95±0.07	3.3	1.18
4	0.93±0.11	1.5	0.78

The image analysis indicates that the treatment of the particles in the plasma jet results both in an increase in the particle sphericity and a decrease in their porous area content and mean size of internal pores. The standard deviation obtained for the shape factor can be explained by the original powder size distribution which brings about different heat treatments in the plasma flow. The powder sample 1 exhibits the highest shape factor with the lowest mean size of internal porosity ; this indicates a good melting state of particles prior to their impact onto the substrate. It is consistent with the order of magnitude of the temperature measured by the DPV2000 system. However, it is preferable to discuss such data in terms of particle dwelling

time and plasma thermal properties since the sets 2, 3 and 4 of the spray conditions exhibit about the same mean temperatures but different melting states.



*Figure 2 : SEM cross-section of collected powders
(a): condition 1, (b): condition 2, (c): condition 3, (d): condition 4.*

- Condition 1: The combination of high hydrogen content (25%vol.) in the plasma-forming gas and high specific plasma enthalpy (Table 1) results in the full melting of particles. Indeed, the hydrogen increases the thermal conductivity of the plasma and thus, improves the plasma-particle heat transfer.
- Condition 2: Despite a velocity similar to that of condition 1, the collected particles are highly porous and less spherical (Table 2). These results illustrate a poor melting state of particles which can be related to the low thermal conductivity (hydrogen content: 5%vol.) and low specific enthalpy of the plasma gas.
- Condition 3: The extension of the particle residence time, due to a low plasma gas flow rate combined with a high specific enthalpy and a good thermal conductivity over 10000K (high He content), slightly improves the plasma-particle heat transfer. The collected particles exhibit an average melting state with a good sphericity and a moderate porosity level.
- Condition 4: The variation of the internal porosity content and pore mean size is consistent with a good melting of particles promoted by the long dwelling time of the in-

flight particles in the plasma jet (low particle velocity). Some hollow particles with a thick wall made up of melted elementary particles of the initial agglomerates can be observed. They probably correspond to large particles with temperature over, but close to, the material melting temperature. Therefore the viscosity of the molten particle is too high to permit the gas included in the particle to escape through the molten shell.

Coating microstructure and porosity

SEM observations of the resulting coatings are reported in Fig. 3. Their microstructure can be interpreted with respect to the in-flight particle characteristics since these characteristics govern the viscosity and kinetic energy of the impacting particles and thus control the flattening and solidification processes [6]. Mac Pherson has shown that if the spreading process is complete before solidification, the flattening degree can be calculated using the Madjeski's formula [7]:

$$D/d = 1.2941 \times Re^{0.2}$$

where d is the average particle diameter, D the resulting lamella diameter, Re (Reynolds number) $= \rho \cdot v \cdot d / \mu$ with v the particle impact velocity, ρ the density of the material (6030 kg/m^3) and μ the molten material dynamic viscosity. Due to the lack of data referring to liquid zirconia viscosity, μ has been estimated by using the equation of Shinoda [8]: μ [kg/m.s] $= 0.0037 \cdot \exp(6100/T(K))$, which has been evaluated through the measurements of YSZ flattening degree.

Table 3: Estimation of the flattening degree using the Madjeski's formula

Sample number	1	2	3	4
Flattening degree D/d	6.12	6.02	5.21	4.17

The sets 1 and 2 of spray parameters are characterized by high particle velocity (Table 1) that bring about an important deformation of the impinging particles, a high flattening degree (Table 3) and thus, thin lamellae. This is consistent with the corresponding SEM micrographs (Fig.3a and 3b) where the lamellar structure is difficult to discern. Conversely, the spray condition 4 that leads to low particle velocity and temperature at impact, leads to a poor flattening of the particles on the substrate. The resulting coating has a marked lamellar microstructure and contains some partially-melted particles (Fig.3d). The observed coarse pores can be related to the pull-out of loosely-bonded particles in the coating during the grinding and polishing stages.

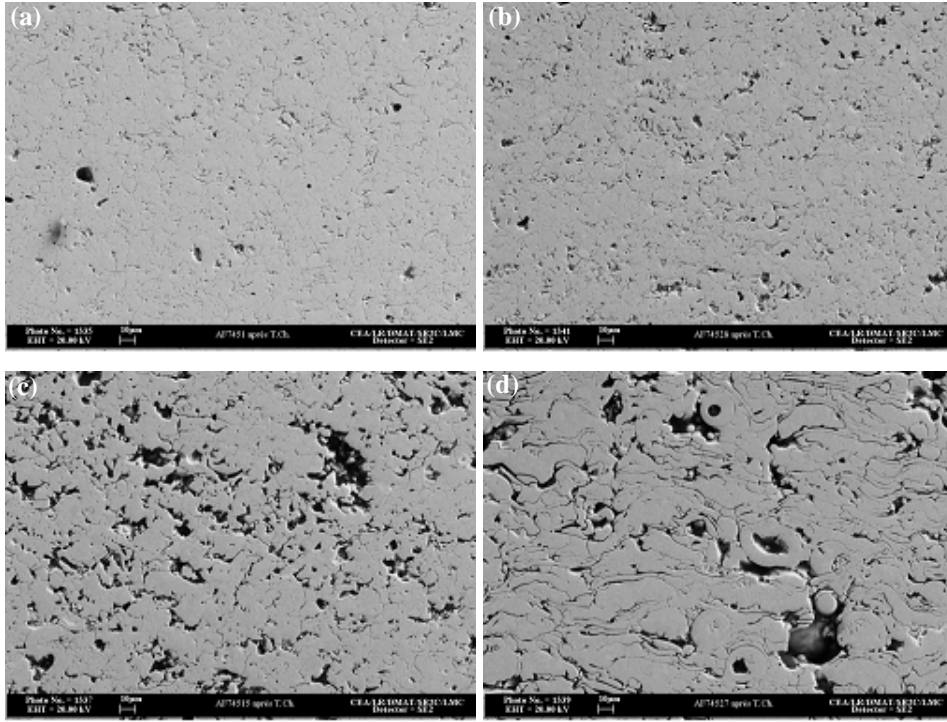


Figure 3: SEM micrographs of YSZ plasma-sprayed coatings (a): coating 1, (b): coating 2, (c): coating 3, (d): coating 4.

The results of the coating porosity estimated by the three methods described before, are given in Table 4. As image analysis failed to measure the submicron-sized pores, the overall pore content is lower except for sample 4 in which pull-outs lead to an overestimation of the porosity value. Thus, the four spray conditions not only lead to a large range of porosity (10-22%) but also to different mean pore size as illustrated in Table 4: coatings 3 and 4 contain micron-sized pores while coatings 1 and 2 have a distribution of submicron-sized pores.

Table 4: Coating porosity features measured with different methods

Sample number	Porosity level			Pore mean diameter (μm) (determined by MIP)
	MIP (%)	Image analysis (%)	Archimedes (%)	
1	11 \pm 1	9.9 \pm 0.4	10.5 \pm 0.4	0.25
2	12 \pm 1	11.8 \pm 0.9	12.3 \pm 0.9	0.2
3	23 \pm 1	22.4 \pm 1.8	22.7 \pm 0.7	1.6
4	18 \pm 1	22.2 \pm 2.7	17.0 \pm 1.0	1

Optical properties

To investigate the radiative properties of the samples, a parameter inversion method has been implemented to calculate the scattering and absorption coefficients. This method involves minimizing the residual sum of squares between the computed reflectance and transmittance derived from the Gouesbet-Maheu four-flux model [9] and from the experimental spectra.

The hemispherical transmittance T and reflectance R measurements have been performed over the 0.5-10 μm wavelength range on freestanding 500 μm -thick coatings annealed at 500 $^{\circ}\text{C}$ during 24h. The transmittance spectra are shown in Fig. 4. The drop in transmittance between 2.5 and 4 μm can be related to the absorption bands of water.

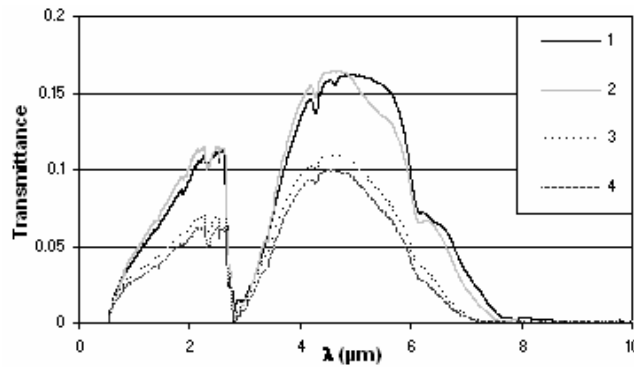


Figure 4 : Transmittance spectra of coatings annealed at 500 $^{\circ}\text{C}$ during 24h

The optical behavior of the YSZ plasma-sprayed coatings can be divided into two wavelength zones according to the variation of the absorption and scattering coefficients (Fig. 5). In region *I* ($\lambda < 5\mu\text{m}$), the plasma-sprayed coatings exhibit a highly scattering feature as reported elsewhere [5]. In region *II* ($5\mu\text{m} < \lambda$), the absorption coefficient becomes high. This is consistent with the increase in the extinction index κ of the YSZ material.

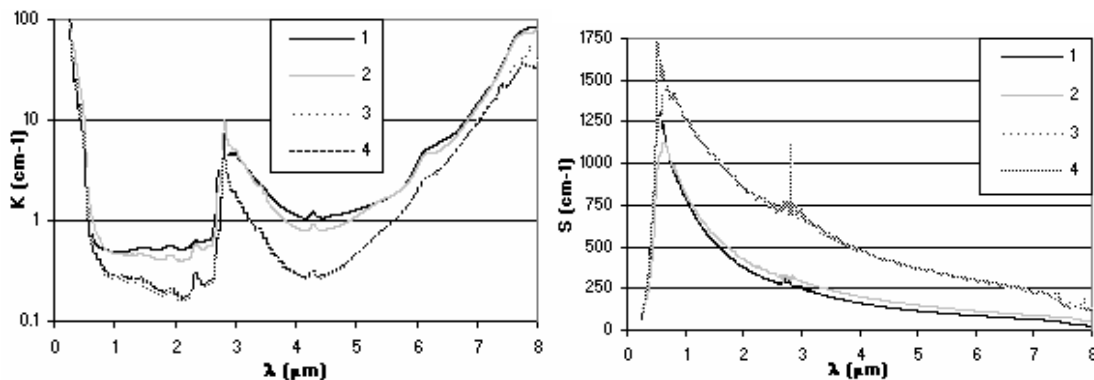


Figure 5: Absorption and scattering coefficients of the YSZ plasma-sprayed coatings

From these variations, two radiative behaviors should be emphasized:

- (1) Coatings 1 and 2 exhibit low backscattering and moderate absorption features: this is consistent with their high transmittance values. By regarding the microstructure features, such a behavior can be related both to the low porosity content (10-12%) and the submicron-sized pores (Table 3).
- (2) Coatings 3 and 4 display lower transmittance spectra due to high backscattering coefficients. This can be attributed both to the high porosity content and the large-sized pores.

These results indicate that the scattering process should be investigated in relation to the porosity features such as the distribution, the mean size and the shape of the pores. The size effect can be interpreted by introducing the pore size parameter x which compares the pore radius r to the wavelength in the matter: $x=(2\pi.r.n_{YSZ})/\lambda$ where n_{YSZ} is the refractive index of YSZ material. When $x<1$, the scattering process decreases as $1/\lambda^4$ (Rayleigh regime) and the distribution of the scattered radiation tends to be isotropic [10] as it is observed for coatings 1 and 2 beyond $1.5\mu\text{m}$. This is consistent with the lower backscattering values and thus the higher transmittance for both coatings while for the coatings 3 and 4 the mean size parameter x is larger than 1 all over the $0.25\text{-}8\mu\text{m}$ range.

Conclusion

In this study, four YSZ plasma-sprayed coatings have been manufactured to establish correlations between the microstructure features and the radiative properties of coatings. The spray parameters have been selected by using two complementary particle diagnostic tools: the DPV2000 system and a particle collecting set-up. The particle melting state has been investigated by studying the cross section of the collected particles. A digital analysis method was used to provide two criteria to quantify the particle melting state: the shape factor and the internal pore features (size and ratio). These results have been discussed in terms of the particle dwelling time in the plasma jet and plasma-particle heat transfer. The resulting microstructures differ in the content, size and shape of pores and thus provide a suitable case study.

The transmittance spectra of these four annealed coatings exhibit consistent differences over the $0.25\text{-}8\mu\text{m}$ wavelength range. The evaluation of absorption and scattering coefficients enables to identify the effects of some pore features such as size and content. To manage efficient thermal barriers, plasma-sprayed coatings with high porosity level and micron-sized pores should be engineered.

A comprehensive study of the radiative properties of YSZ plasma-sprayed coatings requires simplifying the present case by separating the effects of pore size, shape and content. The application of the Mie theory in absorbing media with one-size spherical pores is in progress. To determine the effect of the plasma-sprayed lamellar microstructure, a multilayer model should also be implemented.

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